## Electromagnetics Engineering Handbook

**Analysis and Design of Electrical and Electronic Devices and Systems** 

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#### To our children

# Mahilmany, Elilini, Anbini and Yovahn (SRHH) Vicknesh (KP) Esther, Ezekiel and Elisabeth (PRPH)

#### and to all our students

Great are the works of the LORD; they are studied by all who delight in them. Full of splendor and majesty is His work. (Psalm 111: verses 2, 3a)

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