TWO-PHASE FLOW PHENOMENA IN A HORIZONTAL PIPE WITH A SUDDEN CONTRACTION: EFFECTS OF CONTRACTION RATIO ON FILM BEHAVIOUR

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ABSTRACT
Experimental studies were conducted on the behaviour of water films in a horizontal pipe with a sudden contraction to achieve a fundamental understanding of the film mechanisms of annular flow using high-speed video imaging analysis. The sudden contraction area ratios $Ac = (d_2 / d_1)^2 = 0.36$ and 0.64, where $d_1$ is the inlet pipe diameter (50 mm) and $d_2$ is the contracted pipe diameter were examined. The experiments were carried out for various values of superficial gas and liquid velocities. The superficial gas velocity after mixing ($j_{G1}$) ranged from 18.02 to 24.41 m/s (the calculated velocity from the cross-sectional at the sudden contraction was $j_{G2} = 27.98–67.39$ m/s) and the superficial liquid velocity ($j_{L1}$) ranged from $8.62 \times 10^{-2}$ to $1.23 \times 10^{-1}$ m/s ($j_{L2} = 1.35 \times 10^{-1}–3.42 \times 10^{-1}$ m/s). Four flow regimes were observed after the sudden contraction, namely, huge-wave (HW), two-dimensional disturbance wave (DW1) which is formed perpendicularly to a pipe axis having a distinct coherence, three-dimensional disturbance wave (DW2) which is formed obliquely to the pipe axis, and bow wave (DW3) which is transitional wave to “Misty wave” from DW2. The disturbance wave occurrence frequencies were studied under various conditions of flow rate combination of air and water. DW2 occurs over wide range of the superficial gas and liquid velocities. As the superficial gas velocity and the superficial liquid velocity increase, two-dimensional disturbance waves change into three-dimensional ones. The wave occurrence frequencies in the pipe with the sudden contraction ratio $Ac = 0.36$ were mostly higher than those in the pipe with $Ac = 0.64$.

Keywords: sudden contraction, disturbance wave, flow regime, wave occurrence frequency.

1 INTRODUCTION
Gas–liquid two-phase flows through orifices which are used for controlling pressure or flow rate, are important in multiphase flow measurements [1]. For instance, they are commonly found in pipelines in nuclear power, petroleum, geothermal and food processing industries. In order to predict cavitation erosion rate or improve the measurement accuracy and efficiency, many studies regarding the measurements of two-phase flows have been conducted numerically and experimentally [2]–[5]. A fundamental understanding of the gas–liquid two-phase flow is also essential for designing optimal energy-related apparatus in thermal energy plants, nuclear power plants, chemical plants as well as cooling and heating equipment. Flow pattern changes mainly depend on a number of parameters, such as flow direction, fluid property, flow conditions and channel configurations. Because it is, therefore, necessary to take the flow pattern and regime into account for predicting two-phase pressure drops in different pipe configurations and suitable operating conditions, a number of investigations have been made with regard to the classification of flow patterns in different channel configurations. Chang et al. [6] investigated air–water flows through horizontal and vertical U-bend rectangular channels. They analyzed the two-phase flow patterns by visualizing the interfacial flow transitions through the U-bend in order to understand the pressure drop and the heat transfer process. In addition, the effects of channel height-to-width ratio on the behaviour of air–water flows were demonstrated. They presented that the slug-annular flow in flow pattern maps shifted towards the higher superficial gas velocities as the height-to-width ratio decreased. Air–water flows through horizontal to vertical through a
90-degree bend were analyzed by Saidj et al. [7]. They identified the flow patterns both in the horizontal pipe and the vertical pipe upstream, using the Probability Density Function (PDF) of the time series of the cross sectional averaged void fraction. Hsu et al. [8] examined two-phase flow patterns in 90-degree bends with small diameter tubes. They studied flow patterns in 90-degree bends installed upward horizontally, and downward. They observed a liquid flow reversal and a swirled motion for the upward flow arrangement. Whalley [9] studied air–water flows in a helically coiled tube. They showed the differences in the liquid film thickness and liquid film flow rate around the tube periphery between presented flows and vertical annular flows. Azzopardi and Whalley [10] investigated the effects of flow patterns in a T junction. They found that the entering flow direction of air–water flows was strongly dependent on the flow patterns upstream the junction. Saisorn and Wongwises [11] compared air–water flows through a horizontal circular micro-channel with two-phase flow through ordinarily size channels. They classified the observed flow patterns into three flow regimes and showed comparisons of the observed flow patterns with the flow regime maps proposed by some previous researchers. Few reports, however, have focused on the film mechanism of an annular mist flow in a horizontal pipe with a sudden contraction. Schmidt and Friedel [12] conducted extensive pressure drop measurements across a sudden contraction and provided a new pressure drop model. Chen et al. [13] studied the pressure drops and flow pattern changes across sudden contractions in small rectangular channels having different area ratios. However, a clear understanding of flow patterns is still expected and it is necessary to predict flow-pattern transitions in a horizontal pipe with a sudden contraction due to their physical and practical significance, as well as their feature complexity.

The authors have reported the flow regime transitions in a horizontal pipe with a sudden contraction and measured the water-drop size in the annular mist flow using immersion liquid method [14], [15]. In this paper, the effects of the contraction area ratio on film behaviour were investigated by flow observations and measurements of disturbance wave occurrence frequency in order to contribute the fundamental data concerning to film characteristics in air–water horizontal annular two-phase flow with a sudden contraction.

2 EXPERIMENTAL SET UP

A schematic diagram of the experimental apparatus is shown in Fig. 1. Compressed air was supplied from a compressor to the mixing device where it combines with water from a storage tank. The mixing device consisted of an annular section surrounding a porous sinter wall. The test section was made of transparent acrylic resin in order to allow flow behaviour observations and consisted of an inner diameter pipe $d_1 = 50$ mm, 4320 mm long upstream and $d_2 = 30$ mm or 40 mm downstream the horizontal system. The contraction area ratios $A_c = (d_2 / d_1) ^ 2$ were obtained to be 0.36 and 0.64.

The experiments were carried out for various values of superficial gas and liquid velocities. The superficial gas velocity after mixing ($j_{G1}$) ranged from 18.02 to 24.41 m/s (the calculated velocity from the cross-sectional at the sudden contraction was $j_{G2} = 27.98$–67.39 m/s) and the superficial liquid velocity ($j_{L1}$) ranged from $8.62 \times 10 ^ 2$ to $1.23 \times 10 ^ 3$ m/s ($j_{L2} = 1.35 \times 10 ^ 1$–$3.42 \times 10 ^ 1$ m/s) as summarised in Tables 1 and 2. The superficial gas and liquid velocities were calculated from mass flow rates ($G_A$ and $G_L$), which were obtained from the changes ($h_A$ and $h_L$) in pressure head upstream through a quadrant edged nozzle with the flow coefficients ($\alpha$). The inlet temperature was measured using thermocouples to obtain the density and viscosity, from which the Reynolds numbers ($Re_G$ and $Re_L$) were calculated as shown in Tables 1 and 2. A detailed flow observation using a high-speed video
Table 1: Summary of the experimental conditions of gas phase.

<table>
<thead>
<tr>
<th>$h_A$ mmAq</th>
<th>$G_A$ kg/s</th>
<th>$\alpha$</th>
<th>$j_{G1}$ m/s</th>
<th>$j_{G2}$ m/s</th>
<th>$Re_{G1}$</th>
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<tr>
<td>250</td>
<td>$4.23\times10^{-2}$</td>
<td>0.779</td>
<td>18.02</td>
<td>27.98</td>
<td>49.75</td>
</tr>
<tr>
<td>350</td>
<td>$5.02\times10^{-2}$</td>
<td>0.783</td>
<td>21.45</td>
<td>33.30</td>
<td>59.21</td>
</tr>
<tr>
<td>450</td>
<td>$5.72\times10^{-2}$</td>
<td>0.786</td>
<td>24.41</td>
<td>37.90</td>
<td>67.39</td>
</tr>
</tbody>
</table>

Table 2: Summary of the experimental conditions of liquid phase.

<table>
<thead>
<tr>
<th>$h_L$ mmAq</th>
<th>$G_L$ kg/s</th>
<th>$j_{L1}$ m/s</th>
<th>$j_{L2}$ m/s</th>
<th>$Re_{L1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>50</td>
<td>$1.67\times10^{-1}$</td>
<td>8.62$\times10^{-2}$</td>
<td>1.35$\times10^{-1}$</td>
<td>2.39$\times10^{-1}$</td>
</tr>
<tr>
<td>55</td>
<td>$1.76\times10^{-1}$</td>
<td>9.00$\times10^{-2}$</td>
<td>1.41$\times10^{-1}$</td>
<td>2.50$\times10^{-1}$</td>
</tr>
<tr>
<td>60</td>
<td>$1.84\times10^{-1}$</td>
<td>9.47$\times10^{-2}$</td>
<td>1.48$\times10^{-1}$</td>
<td>2.63$\times10^{-1}$</td>
</tr>
<tr>
<td>65</td>
<td>$1.91\times10^{-1}$</td>
<td>9.80$\times10^{-2}$</td>
<td>1.53$\times10^{-1}$</td>
<td>2.72$\times10^{-1}$</td>
</tr>
<tr>
<td>70</td>
<td>$1.99\times10^{-1}$</td>
<td>1.03$\times10^{-1}$</td>
<td>1.60$\times10^{-1}$</td>
<td>2.85$\times10^{-1}$</td>
</tr>
<tr>
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<td>$2.06\times10^{-1}$</td>
<td>1.06$\times10^{-1}$</td>
<td>1.65$\times10^{-1}$</td>
<td>2.93$\times10^{-1}$</td>
</tr>
<tr>
<td>80</td>
<td>$2.13\times10^{-1}$</td>
<td>1.10$\times10^{-1}$</td>
<td>1.72$\times10^{-1}$</td>
<td>3.05$\times10^{-1}$</td>
</tr>
<tr>
<td>85</td>
<td>$2.19\times10^{-1}$</td>
<td>1.13$\times10^{-1}$</td>
<td>1.76$\times10^{-1}$</td>
<td>3.13$\times10^{-1}$</td>
</tr>
<tr>
<td>90</td>
<td>$2.23\times10^{-1}$</td>
<td>1.17$\times10^{-1}$</td>
<td>1.82$\times10^{-1}$</td>
<td>3.24$\times10^{-1}$</td>
</tr>
<tr>
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<td>1.19$\times10^{-1}$</td>
<td>1.86$\times10^{-1}$</td>
<td>3.31$\times10^{-1}$</td>
</tr>
<tr>
<td>100</td>
<td>$2.38\times10^{-1}$</td>
<td>1.23$\times10^{-1}$</td>
<td>1.92$\times10^{-1}$</td>
<td>3.42$\times10^{-1}$</td>
</tr>
</tbody>
</table>
camera revealed the flow regime transitions at $z_2/d_2 = 10, 40$ and $80$ denoting the normalised streamwise distance from the sudden contraction. Passing frequencies of disturbance waves were measured for ten minutes by visual observations at every measurement point under each condition. The average values of the measured frequencies which were taken for three minutes; one minute at the beginning, at the middle and at the end of the measurements, were used as disturbance wave occurrence frequencies, which will be explained in Section 3.2.

3 RESULTS AND DISCUSSIONS

3.1 Flow regime

The flow regime transitions were examined to elucidate the developing process of the two-phase flow. In a horizontal pipe a number of different flow patterns may be observed depending on the conditions of the flow rate combination of air and water [16]. Fig. 2(a) shows “Stratified flow” in which the two phases flow separately with a relatively smooth interface at low gas and liquid velocities. Fig. 2(b) shows “Wavy flow” in which the interface becomes disturbed by waves traveling in the direction of flow. At high gas flow rates the liquid flows in an annular film on the pipe wall with the gas moving rapidly in a central core. At low liquid flow rates the film is relatively smooth with small ripples as shown in Fig. 2(c). The liquid became entrained into the gas in droplet form, resulting Fig. 2(d). As the liquid rate is increased the surface of the film becomes distorted with the formation of “Huge waves” and “Disturbance waves”.

![Flow regime in horizontal flow.](image)

**Figure 2:** Flow regime in horizontal flow. (a) Stratified flow; (b) Wavy flow; (c) Ripple; (d) Quasi-ripple; (e) Huge wave (HW); (f) Two-dimensional disturbance wave (DW1); (g) Three-dimensional disturbance wave (DW2); (h) Quasi-bow wave (DW3); and (i) Misty wave.

An annular mist flow, in which a liquid flows on the wall of a pipe as a film and a gas flows in the centre [17], was observed after the sudden contraction in the present experimental range, while “Wavy flow” was observed before the sudden contraction. The visual observation allowed a more detailed classification of the annular mist flows. Some
photos of observed typical flow regimes are shown in Fig. 3. Four flow regimes were observed; huge-wave (HW), two-dimensional disturbance wave (DW1), three-dimensional disturbance wave (DW2) and quasi-bow wave (DW3) which was a transitional wave to “Misty wave” from DW2. DW1 is formed perpendicularly to the pipe axis and coherent [18] around the pipe circumference, while DW2 is distorted in the streamwise direction, then a part of the ringwise waves begins to be broken. These waves with no coherence around the pipe circumference three-dimensional disturbance waves were termed DW2, as distinguished from DW1. At high gas and liquid velocities, DW3 which was transitional wave to “Misty wave” from DW2 was observed. DW3 is a comparable wave to “Bow wave” which has been observed in the literature [18] for two-phase flow through a large diameter vertical pipe.

![Photos of typical flow regime. (a) HW; (b) DW1; (c) DW2; and (d) DW3.](image)

Figs 4 and 5 show the observed flow regime maps at $z_2/d_2 = 10, 40, 80$ downstream the sudden contraction for the air–water flows in a horizontal pipe with a sudden contraction of $A_c = 0.36$ and 0.64, respectively. The flow pattern transition curves suggested by Mandhane et al. [19] and Taitel et al. [20] are illustrated by broken lines in Figs 4 and 5. The observed flows under the experimental conditions were categorized as annular regimes by them and classified more in detail into four flow regimes, as mentioned above. The flow regime DW1+DW2 is observed and subsequently DW1+DW2+DW3, DW2+DW3 as the superficial gas and liquid velocities increase in Fig. 4. Moreover, as the normalized axial distance $z_2/d_2$ increases up to 80, the flow regime shifts from DW1+DW2 to DW1+DW2+DW3 at the same $j_{G1}$ and $j_{L1}$. DW1 region narrows and alternately DW3 region widens toward downstream after the sudden contraction. In Fig. 5(a) and (b), as the superficial gas and liquid velocities increase, the flow regime DW1+DW2 is observed and subsequently DW1+DW2+DW3, which is the similar evolution occurred in Fig. 4, expect that no flow regime of DW2+DW3 is observed in Fig. 5. Fig. 5(c), in contrast, indicates the existence of HW. The flow regime HW+DW1+DW2 is observed at low $j_{G1}$ and high $j_{L1}$, $z_2/d_2 = 80$ in Fig. 5(c). HW occurrence at lower $j_{G1}$ is observed at lower $j_{L1}$. When DW3 occurs, HW disappears.
Figure 4: Flow regime map for $A_C = 0.36$.

Figure 5: Flow regime map for $A_C = 0.64$. 
3.2 Effect of the superficial gas velocity on mean frequencies for disturbance wave

Fig. 6(a) and (b) show the change in the mean frequency of disturbance wave occurrence with the superficial gas velocity \( j_{G1} \) at \( j_{L1} = 1.10 \times 10^{-1} \text{ m/s} \), \( z_2/d_2 = 20 \) and 80, respectively. The authors define the wave occurrence frequency as the mean number of waves per second passing an arbitrary point in the pipe. The frequencies of \( DW_1 \), \( DW_2 \), \( DW_3 \) and \( DW \): the sum of these frequencies, are denoted by \( f_{D1} \), \( f_{D2} \), \( f_{D3} \) and \( f_D \), respectively.

![Figure 6(a) and (b) showing the change in mean frequency of disturbance wave occurrence with superficial gas velocity.](image)

(a) and (b) show the change in the mean frequency of disturbance wave occurrence with the superficial gas velocity \( j_{G1} \) at \( j_{L1} = 1.10 \times 10^{-1} \text{ m/s} \), \( z_2/d_2 = 20 \) and 80, respectively. The authors define the wave occurrence frequency as the mean number of waves per second passing an arbitrary point in the pipe. The frequencies of \( DW_1 \), \( DW_2 \), \( DW_3 \) and \( DW \): the sum of these frequencies, are denoted by \( f_{D1} \), \( f_{D2} \), \( f_{D3} \) and \( f_D \), respectively.

Figure 6: Effect of the superficial gas velocity on mean frequencies for disturbance waves \( (j_{L1} = 1.10 \times 10^{-1} \text{ m/s}) \). (a) \( z_2/d_2 = 20 \); and (b) \( z_2/d_2 = 80 \).

The mean frequency values obtained in flows through the sudden contraction of \( A_C = 0.36 \) are higher than those in the case of \( A_C = 0.64 \). \( DW_2 \) occurs over wide range of the superficial gas and liquid velocities in the both cases of \( A_C = 0.36 \) and 0.64. \( DW_2 \), \( DW_3 \) and \( DW \) increase with the superficial gas velocity. \( DW_1 \), in contrast, decreases with \( j_{G1} \). \( DW_3 \) is observed at high velocity \( j_{G1} \). At \( z_2/d_2 = 80 \) as shown in Fig. 6(b), the frequencies of \( DW_2 \) and \( DW \) for \( A_C = 0.36 \) are nearly constant up to the superficial gas velocity 21.45 m/s and decrease at \( j_{G1} = 24.45 \text{ m/s} \), while the frequency of \( DW_3 \) slightly increases. Thus, \( DW_2 \) decreases after the appearance of \( DW_3 \). On the other hand, the frequency of \( DW_2 \) and \( DW \) for \( A_C = 0.64 \) gradually increase. The increasing rate of \( DW \) at \( z_2/d_2 = 80 \) is smaller than that at \( z_2/d_2 = 20 \). The increasing rate of \( DW \) caused by the increasing \( j_{G1} \) is moderated with increasing \( z_2/d_2 \).
3.3 Effect of the superficial liquid velocity on mean frequencies for disturbance waves

Fig. 7(a) and (b) show the change in the mean frequency of disturbance wave with the superficial liquid velocity \( j_{L1} \) at \( j_{G1} = 21.45 \text{ m/s} \), \( z_2/d_2 = 20 \) and 80, respectively.

![Figure 7](image)

Figure 7: Effect of the superficial liquid velocity on mean frequencies for disturbance waves \((j_{G1} = 21.45 \text{ m/s})\). (a) \( z_2/d_2 = 20 \); and (b) \( z_2/d_2 = 80 \).

The frequencies of DW_2 and DW for \( A_C = 0.36 \) increase constantly. DW_1 occurs more frequent than DW_3 does, although their occurrence frequencies are much smaller than that of DW_2. On the other hand, the frequencies of DW_2 and DW for \( A_C = 0.64 \) are nearly constant up to \( j_{L1} = 1.13 \times 10^{-1} \text{ m/s} \) and increase rapidly as the superficial liquid velocity increases. DW_1 and DW_3 occur over wide range of the superficial liquid velocity, although the occurrence frequencies of them are much smaller than that of DW_2. Fig. 7(a) clearly indicates effects of the contraction area ratio at low superficial liquid velocity.

Fig. 7(b) indicates that little influence of the sudden contraction area ratios on the mean frequencies of disturbance waves are observed. The frequencies of DW_2 in the both cases of \( A_C = 0.36 \) and 0.64 increase with the superficial liquid velocity. It follows that the frequency of DW increases constantly. DW_3 for \( A_C = 0.36 \) is observed over wide range of the superficial liquid velocity at \( z_2/d_2 = 80 \), while DW_1 occurs at \( z_2/d_2 = 20 \). The mean frequency distributions become similar as \( z_2/d_2 \) increases.
3.4 Mean frequencies for disturbance waves in the normalized axial direction

Fig. 8 shows the mean frequencies for disturbance waves in the normalized axial direction. DW for $A_C = 0.36$ continually decreases, while that for $A_C = 0.64$ decreases up to $z_2/d_2 = 20$ and then stays quasi constant. DW$_2$, which mainly occurs in the normalized axial direction, decreases in a similar way as DW. DW$_1$ is much less than DW$_2$ and disappears at the downstream. DW$_3$ gradually increases in the downstream. The change tendency of disturbance waves with $j_{G2}$ and $j_{L2}$ are qualitatively the same in the experimental ranges.

![Figure 8: Mean frequencies for disturbance waves in the normalized axial direction.](image)

**4 CONCLUSIONS**

The effects of the contraction area ratio on film behaviour of two-phase flow in a horizontal pipe were investigated. The following main results were obtained in the experimental conditions.

1. Four flow regimes were observed; huge-wave, two-dimensional disturbance wave, three-dimensional disturbance wave and quasi-bow wave.
2. The flow regime transits from DW$_1 +$ DW$_2$ to DW$_1 +$ DW$_2 +$ DW$_3$ as the superficial gas and liquid velocities increase. In the case of $A_C = 0.36$, DW$_2 +$ DW$_3$ is observed and the transition occurs at lower superficial gas and liquid velocities in contrast to the case of $A_C = 0.64$.
3. The effects of the contraction area ratio become less as $z_2/d_2$ increases.
4. DW$_2$ occurs mainly in the both cases of $A_C = 0.36$ and 0.64. The wave occurrence frequencies in the pipe with the sudden contraction ratio $A_C = 0.36$ were mostly higher than those in the pipe with $A_C = 0.64$.

**REFERENCES**


