Rheological properties and debris-flow modeling in a southern Italy watershed

T. Bisantino¹, P. Fischer², F. Gentile¹ & G. Trisorio Liuzzi¹
¹PROGESA Department, University of Bari, Italy
²ETH Zurich, Institute of Food Science and Nutrition, Switzerland

Abstract

The Pulsano watershed, located in the southern side of Gargano (Puglia-Italy), is subject to debris-flow phenomena originating from the weathering of the limestone rocks that constitute the geological parent material. The territory is poorly monitored and between intense and rare events, which transport large particle size materials, more frequent hyper-concentrated flows, which transport heterogeneous sediments, occur. On this basis the debris-flow risk assessment appears very complex, since it depends on both the available debris volume and the hydraulic characteristics of the flow. This work proposes a methodology of analysis and modeling of debris-flows that is able to integrate the results of the experimental investigations on materials with models simulating the triggering, propagation and deposition of the flow. For this purpose the rheological response of natural suspensions collected from the superficial deposits was investigated using a rheometric tool for large particle suspensions: the Ball Measuring System (BMS). The triggering and propagation of the debris-flow were simulated using the SHALSTAB and FLO-2D models in order to reproduce the 15 July 1972 event. Afterwards the influence of rheology on debris-flow depositional features was investigated.

Keywords: debris-flow, rheology, modeling.

1 Introduction

In recent years some debris-flow events occurred in the South-Gargano watersheds (Puglia Region-Southern Italy). These phenomena originate from the weathering of the limestone rocks that constitute the geological parent material
of the promontory and are fostered by the inadequate protection of the degraded forests.

In this work an integrated approach for debris-flow analysis and modeling was set up to study the poorly documented event of July 1972, which occurred in the Pulsano watershed (Gentile et al. [1]). The methodology uses a physically-based model (SHALSTAB, Montgomery and Dietrich [2]), which identifies the areas of potential shallow landsliding, and a two-dimensional debris-flow routing model (FLO-2D, O’Brien et al. [3]) that calculates depths, velocities and runout distances of the mixture.

The geo-mechanical and rheological properties of the materials involved in debris-flows were investigated as they represent key factors for physical and numerical modeling of the debris-flow dynamic. To define the geo-mechanical behavior of the soil a first batch constituted of ten soil samples was collected from the Pulsano watershed (Gentile et al. [4]). For the rheological experiments a second batch, constituted of four soil samples, was selected and analyzed using a rheometric system for fluids with large particle size: the ball measuring system (BMS) (Schatzmann et al. [5], Bisantino et al. [6]). The Bingham rheological model was fitted to the experimental data. The results of the experiments were analyzed with reference to the sediment concentration.

The output of debris-flow modeling was compared with field observations. Finally, the depositional features of the debris-flows were investigated varying the rheological parameters.

2 Materials and methods

2.1 Debris-flow modeling

The total debris volume triggered by heavy rains can be estimated using empirical formulas (Takei [7], Kronfellner-Kraus [8], PWRI [9], D’Agostino et al. [10], Marchi and Tecca [11], Marchi and D’Agostino [12], Tropeano and Turconi [13]), geomorphologic approaches (Hungr et al. [14]), or stability models such as SHALSTAB (Montgomery and Dietrich [2]), SINMAP (Pack et al. [15]), LISA (Hammond et al. [16]), and the one developed by Iverson [17].

The efficacy of the empirical formulas is limited by the variability of debris-flow phenomena and by the sediment availability (Rickenmann [18]). On the other hand the geomorphologic approach is influenced by the evaluation of the debris material that can be mobilized (Brochet et al. [19]). Physically-based modeling is an important tool for magnitude assessment as it considers the hydraulic, morphologic and geo-mechanical properties of materials during the event.

SHALSTAB is a coupled hydrologic and slope stability model that assumes steady state and saturated flow parallel to the slide surface. It states that shallow landslides are influenced by the topography, the convergence of subsurface runoff, the saturation degree of materials and the reduction of the shear stress in the granular mixture. The coupled model is represented by the following equation:
Q = \frac{T \cdot \theta}{a \cdot b} \left[ \frac{c}{\rho \cdot g \cdot z \cdot \cos \theta \cdot \tan \phi} + \frac{\rho_s \cdot (1 - \tan \theta)}{\rho_w \cdot \tan \phi} \right]

where \( a \) is the drainage area, \( b \) is the outflow boundary length, \( \theta \) is the hillslope angle, \( T \) is the transmissivity, \( Q \) is the effective rain, \( \rho_s \) is the soil density, \( c \) is the cohesion and \( \phi \) is the friction angle.

The FLO-2D model was used to perform the runout modeling. It is based on the solution of the conservation of mass and momentum equations and uses a quadratic rheological model defining the flow pattern of the mixture both for a viscous fluid and for a turbulent/dispersive fluid. The resistant term of the Saint Venant equations has a higher influence on reproducing debris-flows than the other terms (Arattano et al. [20]), so it should be adequately estimated. The rheological behavior of a debris-flow containing coarse particles cannot be assessed considering exclusively the contribution of the finer matrix (silt and clay) and thus neglecting the effects of direct grain contacts (Sosio et al. [21]).

2.2 Rheological parameters

The rheology of a suspension can be analyzed through measurements of shear stress \( \tau \) at various shear rate \( \dot{\gamma} \). These parameters have been investigated by several authors, for different debris mixtures, through laboratory systems such as parallel plates, concentric cylinder rheometers, slump test, inclined plane test and belt conveyor (Coussot and Piau [22], Malet et al. [23]).

Fine sediment mixtures at low concentrations show a Newtonian behavior whereas at higher concentrations they have a viscoplastic behavior represented by the Bingham (yielding with subsequent Newtonian flow), Herschel-Bulkley (yielding with subsequent power-law flow) models, bilinear (Locat [24]), (Newtonian flow at low shear stress and Bingham flow at high shear stress), quadratic (O’Brien et al. [3]). The last model describes the continuous flow regimes from viscous to turbulent/dispersive flow:

\[
\tau = \tau_y + \eta \cdot \dot{\gamma} + C \cdot \dot{\gamma}^2
\]

where \( \tau \) is the shear stress, \( \tau_y \) the yield stress, \( \dot{\gamma} \) the shear rate, \( \eta \) the dynamic viscosity and \( C \) is the inertial shear stress coefficient (Bagnold [25]). For mixtures having a mainly viscous behavior the quadratic term can be neglected and the model leads to the Bingham one. The viscosity \( \eta \) and the yield stress \( \tau_y \) are expressed as an exponential function of the volumetric concentration of fine sediments:

\[
\eta = \alpha_1 e^{\beta_1 C_v}
\]

\[
\tau_y = \alpha_2 e^{\beta_2 C_v}
\]

where \( \alpha_i \) and \( \beta_i \) are empirical coefficients defined in experiments.
In recent years, debris-flow materials containing large size particles have been examined. The results show that: the Herschel-Bulkley model can fit the data and that the exponent \( n \) and the ratio \( k/\tau_c \) of the equation remain constant for suspensions obtained adding coarse particles to a large content of fine fraction (Coussot et al. [26]); for shear rates > 10 s\(^{-1}\) the Bingham model obtains better results than the Herschel-Bulkley one (Hübl and Steinwendtner [27]), meaning that the material under flow behaves more Newtonian than shear-thinning; at the same concentrations \( C_v \) gravel-mud mixtures having a larger content of fine sediments (d<1mm) have higher values of viscosity and yield stress (Wang and Jan [28]).

A recently developed rheometrical tool, the ball measuring system (BMS), has been used to analyze fine and large particle suspensions (Schatzmann et al. [29]). In the BMS the dragged measuring sphere can be considered as a particle on which the interactions with the fluid or the other particles are measured. A comparative analysis between the BMS, large-scale rheometers, and other commonly accepted methods was performed using debris-flow materials taken from Eastern Switzerland (Kaitna et al. [30]). The experiments, involving mixtures with different concentrations and particle size up to 5 mm, demonstrated that the results of the experiments obtained with the BMS are quite consistent with those obtained with large-scale rheometers, slump test, and inclined plate tests.

### 2.3 Study site and input data

The study was applied to map the flooded areas of the Pulsano torrent during the July 1972 storm event. The area extends from the Gargano promontory (altitude\(_{\text{max}} = 880\) m a.s.l.) down to the alluvial fan where the agricultural and industrial areas of Manfredonia spread, fig. 1.

The torrent has a watershed characterized by erosion processes on the hillslopes, failing stone walls, scouring and bank failure along the hydrographic network. The parent material of the watershed is mainly composed by dolomitic limestone (Triassic-Cretaceous era). Some field surveys and laboratory tests were carried out on the colluvial deposits to evaluate the geo-mechanical properties of the soil matrix that belongs to the class of loamy-sand materials, tab. 1.

The vegetal cover is characterized by natural grazing, prairies and broad-leaved woods at high altitudes; olive trees, crops and natural areas in the alluvial fan. The climate is typically Mediterranean, with rainfalls ranging from 450 to 780 mm/year and average temperature ranging from 10 to 16°C. On July 15, 1972 a catastrophic debris-flow inundated Manfredonia. Four valleys within the town turned into conveyance channels and the flow reached depths \( h > 1.25 \) m as mapped by Bissanti [31], fig. 2. The estimated return period of the rainfall is \( T_r > 200 \) years.

Four soil samples, collected from the Pulsano watershed, were selected for the rheological tests. The samples contain high amount of large particles (d < 4 mm) and some clasts with a diameter > 4 mm. The clasts create jamming
Figure 1: The Pulsano watershed.

Table 1: Main characteristics of the Pulsano watershed. Physical and mechanical properties of the soil.

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basin area A</td>
<td>15.6 Km²</td>
</tr>
<tr>
<td>Mean altitude hₘ</td>
<td>464.0 m a.s.l.</td>
</tr>
<tr>
<td>Main channel slope i</td>
<td>17.5 %</td>
</tr>
<tr>
<td>Mean alluvial cone slope Sᶠ</td>
<td>14.0 %</td>
</tr>
<tr>
<td>Cohesion c</td>
<td>2500 N/m²</td>
</tr>
<tr>
<td>Angle of internal friction φ</td>
<td>31 °</td>
</tr>
<tr>
<td>Saturated hydraulic conductivity kₚ₅</td>
<td>10-6 m/s</td>
</tr>
<tr>
<td>Volume unit weight γₛ</td>
<td>1430 Kg/m³</td>
</tr>
</tbody>
</table>

of the rotating ball of the rheometer, cause rapid sedimentation, and large scattering of viscosity readings when the measuring tool is interacting with the particles. To better perform the rheological measurements the samples were sieved with a cut-off of 4 mm (very fine gravel), a method justified by the results of Schatzmann et al. [5] and Schatzmann et al. [29]. The matrix consists of moderately sorted sand to very fine gravel and low mud content. The grain size distribution of each sample is reported in figure 3. The samples were examined considering a fixed water content representing the actual debris-flow conditions and in fully water-saturated conditions, tab. 2.
In order to calculate the total debris mobilizable volume a 10 m grid DEM of the Pulsano watershed was used. Using field surveys and photo interpretation, the thickness of the deposits prone to landsliding was evaluated and combined with the results of the stability model SHALSTAB to get the potentially unstable volumes. The inflow debris-flow hydrograph was computed by means of a rainfall-runoff analysis and combined with a variable distribution of the sediment concentration. The computational domain used for the 2D debris-flow modeling was obtained from a 90 m grid DEM. A second 5 m grid system was used to define the cross-section geometry of the torrent and a road network was added to complete the map.
3 Results

The rheological parameters (viscosity $\eta$ and shear stress $\tau$) of the samples collected in the Pulsano watershed were estimated for different sediment concentrations $C_v$. At $C_v=0.42$ eight different shear rates ($0.1, 0.3, 0.5, 1, 3, 5, 10,$ and $30 \, s^{-1}$) were performed. The samples showed a similar shear-thinning flow behavior (viscosity decreases with shear rate). Plotting the average curve of all samples, a good estimate of the viscosity of the debris-flow material was obtained. In water-saturated conditions ($C_v \approx 0.8$) four different shear rates ($0.1, 1, 10,$ and $30 \, s^{-1}$) were performed. The results confirmed the shear-thinning flow behavior of the mixtures.

The Bingham model was fitted to the shear stress data to derive the Bingham viscosity and yield stress. At shear rates lower than $0.1 \, s^{-1}$ measurements were influenced by sedimentation (the tool is then measuring in the more dense lower part of the sample) so they were excluded from the dataset. Figure 4 reports the viscosity (a) and shear stress (b) experimental values, obtained for $C_v = 0.42$ and $C_v = 0.8$, varying the shear rate. The figure also contains the Bingham viscosity and yield stress calculated for both the sediment concentrations.

![Figure 4](image)

(a) Viscosity and (b) shear stress versus shear rate for tests with different $C_v$. The Bingham model fitted to the data.

The empirical relationships between viscosity $\eta$ and $C_v$ and between yield stress $\tau_y$ and $C_v$ were compared with those found in literature, fig. 5. At sediment concentrations $C_v \geq 0.3-0.4$ viscosity and yield stress show different values on the basis of the sediment composition. For example, O’Brien and Julien’s matrices [32], contain only fine sediments ($d < 63 \, \mu m$) and samples having lower clay contents are characterized by lower viscosity and yield stress at the same concentration. Rheological parameters obtained by Hübl and Steinwendtner [33] are related to viscous debris-flows with maximum grain size up to 20 mm. And, finally, the material investigated by Kang and Zhang [34] is a poorly-sorted silt for which a lower sensitivity of the rheological parameters to the water content was observed. In this study the viscosity and yield stress values are generally
lower, at the same total sediment concentration $C_v$, than those found in literature and present a low sensitivity to the water content. However, these results are in agreement to the others as the samples have high percentages of sand and low percentages of finer fractions.

Using the mean experimental values of the rheological parameters and the FLO-2D model the inundated areas and water-sediment depths of the 15 July 1972 event were computed. The debris-flow reconstruction is consistent with the estimations based on the existing documentation, fig. 6. The maximum flow depths simulated by the model are quite similar to those reported by the historical map, i.e. $h > 1.25$ m.

The rheological parameters presented in figure 5 (Bisantino et al. [6]) have been used in debris-flow modeling to represent the real inundated area. The results justify the grain size cut-off in rheological measurements and the use of the BMS device when debris matrix contains high percentages of sandy particles. Further modeling was carried out in order to evaluate the depositional features of the coarser fraction. Generally sediment rheology is heterogeneous from head to tail: coarse clasts are concentrated at the head, are relatively dry.

![Figure 5: Viscosity and yield stress dependency on total sediment concentration $C_v$.](image-url)
Debris-flow reconstruction of the 15 July 1972 event: (a) comparison between observed and simulated inundated area; (b) overall calculation. The calculations are based on the rheological parameters obtained with the BMS (Bisantino et al. [6]); (c) debris-flow simulations with increasing yield stress.

and provide much frictional resistance; a more liquefied material follows the head and exhibits lower yield strength (Iverson [35]). The coarse-grained fraction is mainly dominated by frictional grain interactions before the deposition (Sohn [36]). In the modeling the relationship between yield stress and sediment concentration was modified according to O’Brien and Julien [32], (Aspen Pit 1). This assumption determines the increment of yield stress from \( \tau_y \cong 2.5 \, Pa \) to \( \tau_y \cong 100 \, Pa \). The consequence is that the inundated areas are lower and the deposits are concentrated near the stream network, fig. 6, as observed for the coarser material during the survey carried out after the 15 July 1972 event.

# 4 Conclusions

In this study the dynamics and the rheological properties of the debris-flows in the Pulsano watershed (Southern-Italy) were investigated. The estimated debris-flow hydrograph that reproduce the July 1972 event was derived from rainfall-runoff analysis and the application of the stability model SHALSTAB.

The debris-flow material has a sand content up to 80% and lower fractions of gravel and fine sediments. A rheometrical tool (BMS ball measuring system) for large particle suspensions up to 4 mm was chosen to analyze the matrices (Bisantino et al. [6]). The measurements were performed, at different sediment concentrations, on some samples taken from the source and depositional areas. The experimental viscosity and yield stress have a lower sensitivity to the sediment concentrations as the samples contain high amount of particles having grain size \( d > 63 \, \mu m \).

The FLO-2D code used to simulate the debris-flow event well estimated the flow depths and the inundated areas when using the rheological data obtained.
with the BMS. This result confirms the importance of considering the effects of the sandy fraction that mainly constitutes the debris matrix. Yield stress was then increased to evaluate the behavior of the coarse fraction. Depositional areas, simulated by the model, were consistent to those observed after the 15 July 1972 event. The approach adopted in this study can be useful as a part of the analysis involved in the design of the mitigation structures.

References


