SPATIAL CORRELATION OF THE BACKSCATTERED ULTRASONIC GRAIN NOISE IN THE ULTRASONIC INSPECTION OF THE FORGING TITANIUM ALLOY

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ABSTRACT
Ultrasonic inspection is a routine Non Destructive Examination (NDE) method adopted by the aircraft engine manufacturers. However, the detection of smaller defects in such materials is made difficult by the complicated ultrasound-microstructure interactions. One of the adverse influences of the interactions is the high backscattered grain noise level accompanying the ultrasonic inspections of some titanium alloys. The high grain noise deteriorates the Signal to Noise ratio (S/N) of pulse/echo inspections and consequently may lead to the missing detection of an existing flaw. Ultrasonic signal fluctuations have direct impact on flaw detection, flaw characterization and the estimation of the Probability of Detection (POD). The total backscattering is controlled by grain morphology, grain orientation and elastic anisotropy, which may vary throughout the microstructure. Thus any Thermo-Mechanical Processing (TMP) leading to the variations of material microstructure may influence the backscattered grain noise. We developed new ideas of how to extract useful microstructural information from the forging simulation software Simufact.forming, a commercial software package produced by Simufact Engineering GmbH. A model is then developed to correlate the grain noise signals with the microstructural variations due to the inhomogeneous plastic deformation associated with the forging processing. The grain noise levels predicted by the model at various locations are compared with experiments. Reasonably good agreements are observed.

Keywords: ultrasonic grain noise, simulation software, elastic anisotropy.

1 INTRODUCTION
In principle, the noise caused by the structure of polycrystalline materials is the result of the inhomogeneity of the acoustic properties of the material. These in-homogeneities are primarily associated with the anisotropy of the elasticity constants in grains or crystals. Total scattered radiation can be controlled by grain morphology, grain orientation, and elastic anisotropy of the microstructure.

Large variations in material noise were observed in connection with the position and direction of examination for Ti–6Al–4V slabs. Such variations are supposed to be correlated with variations of the microstructure that come from the thermo-mechanical process.

The thermo-mechanical process is the most used way to control the microstructure and consequently the mechanical properties (for example imposing restrictions on the working temperature and the degree of deformation). A large variety of microstructural characteristics of the final product (grain size, degree of recrystallization, texture, etc.) are related to the parameters of thermo-mechanical processes.

Thus, in order to be able to anticipate the ultrasonic behaviour of a material, it is essential to anticipate its structural characteristics as a result of TMP, for which purpose we use computerized prediction techniques of the forging process.
2 MATERIAL NOISE PREDICTION ELEMENTS

A typical thermo-mechanical process is the one applied in the case of forging ingots (Fig. 1). The cast ingot is transformed into a cylindrical billet by reducing the diameter and then by forging it is brought to a shape as close as possible to the final product.

![Figure 1: Typical forging process accompanied by deformation and orientation of the grain depending on their position in the final product [1].](image)

The microstructure of the ticket will depend on the microstructure of the casting and the history of the thermo-mechanical process. In the cast ingot, the grains are typically equiaxed, but due to the drastic reduction in diameter, the typical microstructure of the billet will be with elongated macro-grains (primary $\beta$), consisting of $\alpha$ colonies of hexagonal crystals created by solid state transformations with the orientation determined in the piece of that of the initial $\beta$ grains. The final microstructure of the forging is dependent on the specifics of the forging process (forging temperature, processing time, deformation rate, cooling rate and subsequent heat treatment).

Apart from the morphology of the structure, the in-homogeneities of the plastic deformations during forging induce a preferential orientation of the crystals, a texture formed by the cleavage or maclation of the crystals, or a combination between the two.

Such deformations on which the texture depends will act as the elastic anisotropy factor. $<\delta C_{ij}\delta C_{kl}>$ vary with the position and direction inside the slab. These variations influence the material noise.

Due to these deformations, the deformation texture appears, which is conventionally represented by polar figures that describe the statistical distribution of the hexagonal basal plane. The extent and intensity of the texture are dependent on the volume of deformation and the temperature at which it was performed.

Due to the influence of inhomogeneous plastic deformation, the microstructure is expected to have local variations in grain morphology, grain orientation and texture. However, for large slabs it is difficult to give photographic details of structural variations only through traditional metallographic approaches.

For this purpose there are specialized software packages such as Simufact.forming produced by Simufact Engineering GmbH. An example of using the program Simufact.forming is given in Fig. 2 where the case of a forged cylindrical ticket type is
presented. The figure shows the “stress map” where the variations of the plastic deformation stresses are highlighted according to their position in the part, in a longitudinal section of the forged billet.

![Stress Map](image)

Figure 2: Tension map in a forged ticket section.

An approach was thus developed through a mathematical model that can be predictable from the noise of material deduced from variations in microstructure, which in turn are dependent on plastic deformations during the forging process. It is possible to anticipate and thus determine the noise of the material and implicitly the quality of the material from the point of view of the ultrasonic control, in different areas of a forged part, by modelling the forging technology.

For this purpose, we start from the hypothesis of the elements that cause the scattering of ultrasonic radiation in the bill, having a specific orientation and elongation. These elements are a consequence of the forging process that changes their shape and orientation and introduces the deformation texture. The position and texture of these elements in the slab can be deduced by applying the program Simufact.forming.

2.1 The relationship between the elastic constants of two points located in a textured biphasic microstructure

To predict an absolute noise levels we need detailed knowledge of the metal microstructure which enters the model calculations through certain frequency-dependent factors known as “backscatter coefficients” or “Figures-of-Merit” (FOM). The resulting expression for “noise” produced under these conditions contains a factor which depends on the volumetric density of scatters and their Root Mean Square (RMS) scattering amplitude in the backscattered direction. This term, which is called FOM, appears to be a material property useful in characterizing microstructure. Under the assumption that the solid density is independent of position, FOM (ω) and η (ω) for longitudinal waves propagating in the S3 direction are related to microstructure features by eqn (1):
\[ FOM(\omega)^2 = \eta(\omega) = \frac{K}{(4\pi \rho Vt^2)^2} \int d^3\vec{S} \cdot \delta C_{33}(\vec{r}) \delta C_{33}(\vec{r}') \exp(2i k S), \]  

where:

\( \eta(\omega) \) – backscattering power coefficient,
\( \omega \) – is the angular frequency,
\( k \) – is the magnitude of the wave vector of the incident wave,
\( \rho \) – is the density of the solid,
\( Vt \) – is the longitudinal wave velocity,
\( S = \vec{r} - \vec{r}' \) – is a vector defined by the two points \( \vec{r} \) and \( \vec{r}' \) in the solid medium,
\( S_3 \) – is the component of \( \vec{S} \) in the direction of wave propagation (3-direction),
\( \delta C_{33}(\vec{r}) \) – is the local deviation of the elastic constant from its Voigt average,
\( \delta C_{33}(\vec{r}') \) – \( (C_{33} - C_{33}^{\text{Voigt}}) \), and the notation \( \langle \ldots \rangle \) denotes an ensemble average, and
\( \langle \delta C_{33}(\vec{r}) \delta C_{33}(\vec{r}') \rangle \) is known as the two-point correlation of elastic constants, which describes the correlation in the perturbation in the elastic stiffnesses.

For single-phase materials which are macroscopically homogeneous and have a random microstructure orientation, \( \langle C_{33}(\vec{r}) \delta C_{33}(\vec{r}') \rangle \) may be written in the form:

\[ \langle \delta C_{33}(\vec{r}) \delta C_{33}(\vec{r}') \rangle = \langle \delta C_{33} \delta C_{33} \rangle W(\vec{r} - \vec{r}'), \]  

where:

\( \langle \delta C_{33} \delta C_{33} \rangle \) – is a constant controlled by the crystal anisotropy;
\( W(\vec{r} - \vec{r}') \) – the probability that two points separated by the distance \( \vec{r} - \vec{r}' \) in the solid will be in the same crystal;
\( \langle \delta C_{33} \delta C_{33} \rangle \) can be considered as an average of the solid angle \( (C_{33} - C_{33}^{\text{Voigt}}) \) for a single crystal.

\[ FOM(\omega)^2 = \eta(\omega) = \frac{\omega^2}{4\pi \rho Vt^2} \langle \delta C_{33} \delta C_{33} \rangle > \int d^3\vec{S} \ W(\vec{S}) \exp(2i k S). \]  

For the ellipsoidal element causing scattered radiation shown in Fig. 3, which is assumed to be axially symmetrical along the \( Z \) axis and the semi-axes \( a_m \) and \( c_m \), eqn (3) can be written as in eqns (4)–(7).

\[ FOM(\omega)^2 = \eta(\omega) = \frac{\omega^2}{4\pi \rho Vt^2} \langle \delta C_{33} \delta C_{33} \rangle > \int d^3\vec{S} \ W(\vec{S}) \exp(2i k S). \]  

\[ A = \left( \frac{(1+R^2)-\cos^2 \theta}{(3VR/4\pi)^{1/3}} \right)^2 - 2ik \sin \theta \sin \Phi \sin \tau + \cos \theta \cos \tau, \]  

\[ R = \frac{a_m}{c_m} \] – the ratio of the dimensions of the element causing the scattering and
\[ V = \frac{4\pi a_m^3}{3R} \] – the average volume of the element causing the scattering.
When the variations and intensity of the texture are small, its effect in correlating the elasticity functions between two points is given by the term \( \langle \delta C_{33} \delta C_{33} \rangle \). Due to the presence of texture, this term may change depending on the direction of examination.

The intensity and type of texture are defined as functions of orientation of the crystals, respectively by the probability that a certain crystal has a specific orientation in relation to the coordinate axes of the respective sample.

Specifically, the representation of a crystal in the microstructure is made by a set of Euler angles \( \theta, \psi, \phi \). The orientation function of the crystals is represented by \( w(\xi, \psi, \phi) \), where \( \xi = \cos \theta \) and \( w(\cos \theta, \psi, \phi) \sin \theta \ d\theta \ d\psi \ d\phi \) is the probability of finding crystals oriented in the angular domain \( d\theta \ d\psi \ d\phi \). [1]

Obviously,

\[
\int_{0}^{2\pi} \int_{0}^{2\pi} \int_{-1}^{1} w(\xi, \psi, \phi) \ d\xi \ d\psi \ d\phi = 1. \tag{8}
\]

Once \( w(\xi, \psi, \phi) \) is defined, the effect of the texture can be evaluated. In our case, \( \langle \delta C_{33} \delta C_{33} \rangle \) with texture can be evaluated with eqn (9) [2].

\[
\langle \delta C_{33} \delta C_{33} \rangle = \int_{0}^{2\pi} \int_{0}^{2\pi} \int_{-1}^{1} [\delta C_{33}(\xi, \psi, \phi) \delta C_{33}(\xi, \psi, \phi)] w(\xi, \psi, \phi) \ d\xi \ d\psi \ d\phi. \tag{9}
\]

The term \( \delta C_{33}(\xi, \psi, \phi) \) in eqn (9) represents the local deviation from Voigt’s average of the homogeneous alpha phase macrostructure, respectively \( \delta C_{33}(\xi, \psi, \phi) = C_{33}(\xi, \psi, \phi) - C_{33}\text{Voigt} \). Consider the basal plane of the crystals normal to the flow direction of the metal during plastic deformation, as shown in Fig. 4.

Mathematically, the function \( w(\xi, \psi, \phi) \) is a function only of \( \xi \) or \( \theta (\xi = \cos \theta) \). It is not possible to assess exactly to what extent the distribution of the basal poles changes with respect to \( \theta \). For reasons of mathematical correctness, \( w(\xi) \) is expressed in the Gaussian form \( w(\xi) = Ce^{-(\xi/\Delta)^2} \). By the normalization conditions established in eqn (8), the constant \( C \) is defined in eqn (10), where \( erf \) represents the function error [1].
Figure 4: Crystallite alignment within forging [2].

\[ w(\xi) = \frac{1}{\sqrt{4\pi^2/\Delta_{\text{erf}}} \left( \frac{\Delta}{\Delta} \right)} e^{-\left(\frac{\xi}{\Delta}\right)^2}. \]  

The term \( \Delta \) is the one that determines the intensity of the texture. When \( \Delta \) becomes very large, the texture disappears so that \( w(\xi) \) is a constant for a randomly distributed environment.

The small values of \( \Delta \) correspond to a very pronounced texture. It is known that the intensity of the texture is determined by the volume of labor performed on the material or by the internal stresses resulting from its plastic deformations.

The relation between \( \Delta \) and the internal tensions \( \varepsilon e \) is given by eqn (11).

\[ \Delta = \frac{P1}{\sqrt{\varepsilon e}} \]  

where \( P1 \) is an adjustment parameter that can be deduced by comparing theoretical predictions with a number of experiments. Finally, the function \( w(\xi) \) can be expressed relative to the internal stresses \( \varepsilon e \) according to eqn (12).

\[ w(\xi) = \frac{1}{\sqrt{4\pi^2/P1_{\text{erf}}} \left( \frac{\varepsilon e}{P1} \right)} e^{-\left(\frac{\xi}{\varepsilon e/P1}\right)^2}. \]  

The effect of the texture \( <\delta C33 \delta C33> \) can be evaluated by replacing \( w(\xi) \) in eqn (9) with the expression from eqn (12). A specific example is given by Figs 5 and 6 in which a simulation performed using the program Simufact.forming 12.0., simulation program in the field of forging technologies is presented.
In this case, we started from a Ti6Al–4V ingot with a diameter of 400 mm and forged to a final diameter of 250 mm. Both the map of internal stresses and that of the material flow directions clearly indicate that these directions are rigorously aligned with the radial forging directions. As shown in Fig. 6, the basal plane of the crystals tends to align with the direction of flow of the metal. Since the values of the internal stresses can be evaluated with the help of the stress map obtained with the help of the Simufact.forming program, (Fig. 5) the exact value of $\langle \delta C_{33}\delta C_{33} \rangle$ can be determined with eqn (12) and eqn (9) if $P_1$ is known. For biphasic structures ($\alpha + \beta$), the element $\langle \delta C_{ij}\delta C_{kl} \rangle$ is smaller than that for pure $\alpha$ structures. To quantify this effect, a second adjustment parameter $P_2$ is entered.

$$\langle \delta C_{ij}\delta C_{kl} \rangle_{\alpha + \beta} = P_2 \langle \delta C_{ij}\delta C_{kl} \rangle_\alpha.$$  

(13)

2.2 Calculation of the coefficient of power of the scattered radiation

We consider the model parameter $V$ (eqn (7)) constant in the forging volume while the local parameter $\langle \delta C_{33}\delta C_{33} \rangle_{\alpha + \beta}$ is determined by the two adjustment parameters $P_1$ and $P_2$ and by the plastic deformation stresses (eqns (9)–(13)). The calculation of the FOM is made for the direction of radial examination for tickets and normal to the major surface for forged plates. The values of the internal stresses $\varepsilon_e$ (Fig. 5) and the orientation angles of the crystals in relation to the angle of incidence of the incident beam (Fig. 6) can be determined using the simulation program Simufact.forming, for a specific forging technology, at each point of the examined piece. The FOM calculation is done in several stages, as follows:

**Stage 1 – A FOM-Frequency Dependence Curve** is experimentally raised using the stepped reference block provided with Flat Bottom Holes (FBH) of $\Phi 1.2$ mm and $\Phi 2.0$ mm, positioned at different depths (Fig. 7). To do this, successively scan the FBH $\Phi 1.2$ mm at a depth of 129.5 mm from the inlet surface, with three immersion transducers having the same
dimension of the piezoelectric element but different central frequencies (respectively 2.25 MHz, 5 MHz and 10 MHz) and the oscillograms of each scan are recorded (Figs 8–10).

Figure 6: Map of speeds and flow directions of the material.

Figure 7: Forged plate examination reference block.
The examination sensitivity will be set so that the reference reflector is at the same relative amplitude, respectively FBH Φ 1.2 mm echo at 60% of Full Screen Height (FSH) for each scan. The material noise level (which is directly proportional to the FOM) will be recorded for each transducer and the \( S/N \) ratio for each transducer will be determined. Experimentally, these value of the \( S/N \) ratio are determined as follows:

- 2.25 MHz Transducer – \( S/N = 6:1 \)
- 5.0 MHz Transducer – \( S/N = 4:1 \)
- 10.0 MHz Transducer – \( S/N = 2:1 \)

The Signal/Noise ratio can be expressed as a function of the pulse volume and the power coefficient of the scattered radiation \( \eta (\omega) \) according to eqn (14) [2].

\[
S/N = \left[ \frac{A_{flaw}(\omega)}{\sqrt{\eta(\omega)}} \right] \frac{1}{\sqrt{B^2 \Delta t_p}}
\]  

(14)

where:
- \( B \) – average ultrasonic pulse diameter,
- \( \Delta t_p \) – ultrasonic pulse length and
- \( A_{flaw} \) – amplitude of the reference defect at 60% FSH.
To determine the pulse volume, a FBH Φ1.2 mm located at a depth of 129.5 mm is used for the pulse diameter and the bottom echo from the lower surface of the step of 136 mm (Fig. 7) to determine the pulse length [3].

Given these data and the amplitude of the reference defect A\text{ flaw}, the same (60% FSH) for all examinations, we can determine the conversion factor between FOM and S/N ratio for each transducer, respectively each examination frequency. The dependency graph between FOM and frequency can now be drawn (Fig. 11).

![Figure 11: Dependency FOM-Frequency.](image)

Stage 2 – The Simufact.forming program will be run and the degree of deformation of the material, volume $V$ and ratio $R$ will be set as initial values in order to obtain the values of the plastic deformation stresses $\varepsilon_e$ for the scanned reference block.

Stage 3 – An FOM value will be appreciated from the graph in Fig. 11 for the frequency with which the examination is performed. Using the eqns (3)–(7), from this value determined graphically we can deduce the value $<\delta C3\delta C3>$ from which we can later deduce the value $\Delta$, from eqn (11) and knowing the value $\varepsilon_e$ deduced in Stage 2, the value of the adjustment parameter $P1$ can be deduced.

Stage 4 – Having the value of the adjustment parameter $P1$, and with the help of the simulation program Simufact.forming from which the angle of inclination of the basal plane is extracted in relation to the incident beam $\tau$, volume $V$ and ratio $R$, we can calculate FOM (eqn (4)) for any forged part like the one in Fig. 12, at any point thereof. Since the FOM value is also related to the S/N ratio, for the same transducer and on approximately equal working fields, it can be evaluated by comparing the FOM values obtained by calculation on scan areas 1, 2 and 3 (Fig. 12) with the value obtained on the reference block, which from the areas of the plate to be examined meets the S/N ratio conditions required by the standard.

Another element of material noise prediction is the orientation of the crystals according to the scanning direction. This orientation is related to the direction of flow of the material (Fig. 13) and can be anticipated in order to determine the defining angles for the element causing the scattering (Fig. 3), using the same simulation program. The forging technology will be modified accordingly in order to achieve those material and texture conditions that allow the efficient ultrasonic examination of the semi-finished product.
3 CONCLUSIONS
We set out to develop a model that correlates the material noise with the microstructural variations resulting from the plastic deformations during forging. The inputs of this model refer to the average volume $V$ of the element that causes the scattering, supposed to be constant during forging, to the geometric characteristics of this element and to the local texture due to the inhomogeneity of the plastic deformation stresses.
The shape and orientation of the elements causing the scattering can be deduced with the Simufact.forming simulation program and vary over the entire volume of the slab. The other parameters necessary for modeling, respectively the adjustment parameters $P1$ and $P2$ for the characterization of the anisotropy of the elastic properties were obtained experimentally.

The aim of this paper is a better understanding of the fundamental ultrasonic properties of Ti–6A1–4V slabs as well as the improvement of inspection and manufacturing procedures of this material.

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