

# PRESSURE LOSS OF WATER–CO<sub>2</sub> TWO-PHASE FLOW UNDER DIFFERENT OPERATING CONDITIONS

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## ABSTRACT

In the present study, pipe flows are used to investigate the behavior flow of water–CO<sub>2</sub> mixtures at different pressures and temperatures. The flow rate and pressure of water and CO<sub>2</sub> are changed by using a pump placed ahead of the mixing point. Pressure and temperature levels are recorded by pressure sensors and thermocouples affixed at points along the pipe loop. The flow regimes of two-phase water–CO<sub>2</sub> flow is visualized through transparent tubes using a high-speed camera. After several experiments, it was found that the mean pressure drop along the tube for a water–CO<sub>2</sub> system flow is about 4 kPa/m for water flow rates between 0.4 and 0.7 L/S and CO<sub>2</sub> flow rates between 2.5 and 11 L/S. The maximum inlet pressure for water is 400 kPa and for CO<sub>2</sub> is 3000 kPa. In this experiment, the phase fraction of water is approximately 0.5–0.15 and the phase fraction of CO<sub>2</sub> is around 0.85–0.95. The investigated flow regime under these flow conditions is often intermittent.

*Keywords:* carbon dioxide, water, two-phase flows, pressure loss, transportation.

## 1 INTRODUCTION

Global warming is considered the most challenging issue facing humanity today, with many research studies now focusing on investigating the main cause of this problem. Studying the behavior of carbon dioxide (CO<sub>2</sub>) in its various phases can provide the key to resolving this critical issue. The wide range of CO<sub>2</sub> capture and storage (CCS) methods results in the transport of large quantities of CO<sub>2</sub> from the capturing locations to storage sites. The majority of these transportation processes occur through pipeline networks, where CO<sub>2</sub> can only be transported in a liquid or dense liquid state. This flow is usually a mixture of gas and liquid (i.e. a two-phase flow), although it sometimes contains impurities (i.e. a three-phase flow). Industrially, CO<sub>2</sub> is typically transported in a supercritical condition, which is a state between gas and liquid, with a density like a liquid and a viscosity like a gas. Transporting CO<sub>2</sub> by pipeline differs significantly from transporting natural gas via pipelines because CO<sub>2</sub> is often delivered in a dense liquid phase, whereas natural gas is transported in a dense gas state [1].

There are a number of challenges related to transportation of CO<sub>2</sub> through a pipeline. For instance, one study argues that because widespread applications of CCS need onshore CO<sub>2</sub> transport pipelines set up in populated areas [2], more safety guidelines are required due to pipeline pressure. At high concentrations, CO<sub>2</sub> is toxic and can cause unconsciousness almost instantaneously and respiratory arrest within one minute [3]. The carbon dioxide percentage is very low in normal room air (around 0.04%) [4], but at higher concentrations (>5%), toxicological effects begin in humans and animals. A carbon dioxide concentration of more than 10% may cause convulsions, coma and death, while concentrations of more than 30% can lead to loss of consciousness in seconds [3], [5]. In fact, even when CO<sub>2</sub> is transported in supercritical condition, water is present, along with nitrogen, oxygen, Sulphur oxides, methane, and other impurities [6].

This research also concluded that under normal transport conditions, a water level of 500 ppm is sufficiently low to minimize the risk of free water and hydrate formation. However, when CO<sub>2</sub> is transported above its critical pressure of 71.3 bar, the solubility of



water is above 1300 ppm for a temperature range of  $-10^{\circ}\text{C}$  to  $25^{\circ}\text{C}$ . In offshore pipelines, the temperature of the sea water is nearly always about  $4^{\circ}\text{C}$ . At this temperature, water solubility is above the proposed 500 ppm for pressures above 40 bars [1]. Based on these studies,  $\text{CO}_2$  is always transported together with quantities of water at quantities that usually exceed the recommended ratio.

Other challenges reveal how the transport of  $\text{CO}_2$  must be handled differently from the transport of oil and gas. One of these is that the critical point ( $7.38\text{ MPa}$  at  $31.1^{\circ}\text{C}$ ) and triple point (about  $518\text{ kPa}$  at  $-56.6^{\circ}\text{C}$ ) differ, which indicates that  $\text{CO}_2$  is transported in a dense liquid state, whereas natural gas is transported in a dense gaseous state. Hence, most equipment and pipelines use for transporting natural gas are not suitable for transporting  $\text{CO}_2$  [2].

In summary, previous studies recommended that when transporting  $\text{CO}_2$  above supercritical condition, water content should be minimized to avoid corrosion and hydrate formation. However, when transported through pipelines in supercritical condition,  $\text{CO}_2$  requires safer equipment design, especially in populated areas, in order to protect people against exposure to high concentrations of carbon dioxide. As a result, and for greenhouse applications,  $\text{CO}_2$  needs to be transported at low pressure and with water moisture. In this work, we conduct an experiment to investigate the transporting of  $\text{CO}_2$  in a gas phase at low pressure through a pipeline system.

## 2 THEORETICAL BACKGROUND

It is important to compare experimental results with theoretical calculations by using available empirical correlations. The Reynolds number is considered the most important parameter for flow regime estimations. In multiphase flows, mixing rules can be used to evaluate actual mixture properties such as density, viscosity, and velocity. The Reynolds number is also used in friction factor evaluations along with relative roughness, with the friction factor playing a role in pressure drop calculations.

### 2.1 Superficial velocities

#### 2.1.1 Superficial velocity of liquid

$$U_{Ls} = \frac{q_L}{A}, \quad (1)$$

where  $A$ : cross-sectional area of flow ( $\text{m}^2$ );  $q_L$ : volume flow rate of liquid ( $\text{m}^3/\text{s}$ ).

#### 2.1.2 Superficial velocity of gas

$$U_{Gs} = \frac{q_G}{A}, \quad (2)$$

where  $q_G$ : volume flow rate of gas ( $\text{m}^3/\text{s}$ ).

### 2.2 Mixture velocity

The sum of superficial velocities is called the mixture velocity:

$$U_{mix} = U_{Ls} + U_{Gs}. \quad (3)$$

### 2.3 Slip velocity

In general, gas and liquid tend to flow at different phase velocities in pipe flows.



The relative phase velocity or the slip velocity is defined by:

$$U_S = |U_G - U_L|. \quad (4)$$

The slip velocity is the ability of the phase which is less dense to flow at a greater velocity than the denser phase. We also can describe slip ratio (S) as:

$$S = \frac{U_G}{U_L}. \quad (5)$$

#### 2.4 Phase fraction

The phase fraction of gas and liquid,  $\lambda$ , is defined as:

$$\lambda_L = \frac{q_L}{q_G + q_L}, \quad (6)$$

$$\lambda_G = 1 - \lambda_L, \quad (7)$$

where  $q_L$  and  $q_G$  are the volumetric flow rates of the two phases.

For a slip condition, we can define the true phase fraction for liquid and gas as:

$$\varepsilon_L = \frac{U_L}{U_L + \frac{1}{S}U_G}, \quad (8)$$

$$\varepsilon_G = \frac{U_G}{S.U_L + U_G}. \quad (9)$$

#### 2.5 Two-phase mixing rule

Starting with the mixture density:

$$\rho_m = \rho_L \varepsilon_L + \rho_G \varepsilon_G, \quad (10)$$

the viscosity of gas-liquid mixture can be estimated from the Dukler correlation:

$$\mu_m = \varepsilon_G \mu_G + (1 - \varepsilon_G) \mu_L. \quad (11)$$

Now we can calculate the Reynolds number of the mixture, as follows:

$$Re_m = \frac{\rho_m u_m D}{\mu_m}. \quad (12)$$

#### 2.6 Beggs and Brill method [7]

The Beggs and Brill correlation depends on the mechanical energy balance and in situ average density to determine horizontal flow regimes and calculate pressure gradient. In terms of horizontal flow regime estimations, the method depends on the Froude Number and other specific parameter calculations, as follows:

Froude Number:

$$N_{FR} = \frac{u_m}{\sqrt{gD}}, \quad (13)$$

$$\lambda_L = \frac{u_{SL}}{u_m}, \quad (14)$$

$$L_1 = 316 \lambda_L^{0.302}, \quad (15)$$

$$L_2 = 0.0009252 \lambda_L^{-2.4684}, \quad (16)$$



$$L_3 = 0.10\lambda_L^{-1.4516}, \quad (17)$$

$$L_4 = 0.5\lambda_L^{-6.738}. \quad (18)$$

The horizontal flow regimes used as correlating parameters in the Beggs and Brill approach are segregated, transition, intermittent, and distributed. The following gives the flow regime transitions.

Segregated flow exists if:

$$\begin{aligned} \lambda_L < 0.01 \text{ and } N_{FR} < L_1 \text{ or} \\ \lambda_L \geq 0.01 \text{ and } N_{FR} < L_2, \\ \lambda_L < 0.01 \text{ and } N_{FR} < L_1 \text{ or} \\ \lambda_L \geq 0.01 \text{ and } N_{FR} < L_2. \end{aligned} \quad (19)$$

Transition flow occurs when:

$$\lambda_L \geq 0.01 \text{ and } L_2 < N_{FR} \leq L_3. \quad (20)$$

Intermittent flow exists when:

$$\begin{aligned} 0.01 \leq \lambda_L < 0.4 \text{ and } L_3 < N_{FR} \leq L_1 \text{ or} \\ \lambda_L > 0.4 \text{ and } L_3 < N_{FR} \leq L_4. \end{aligned} \quad (21)$$

Distributed flow occurs if:

$$\begin{aligned} \lambda_L < 0.4 \text{ and } N_{FR} \geq L_1 \text{ or} \\ \lambda_L \geq 0.4 \text{ and } N_{FR} > L_4. \end{aligned} \quad (22)$$

Pressure drop calculations:

$$P_{tf} = P_1 + \Delta P_L + \Delta P_f, \quad (23)$$

where  $P_{tf}$  = Pressure flowing at any location in the pipeline (kPa);  $P_1$  = Pressure at the tubing loop starting-point before two-phase mixing (kPa);  $\Delta P_L$  = Pressure drops through the flow line (kPa);  $\Delta P_f$  = Pressure drops through the fittings (kPa)

$$\Delta P_L + \Delta P_f = f \left( \frac{L}{D} + \sum \frac{L_e}{D} \right) \frac{\rho v^2}{2g}. \quad (24)$$

### 3 EXPERIMENTAL MEASUREMENTS

A multiphase pipe flow loop was used to investigate water–CO<sub>2</sub> flow and to record the flow conditions. The experiments took place at Memorial University in Newfoundland, Canada. The experimental results in this study were compared with theoretical calculations, while the flow regime of gas/liquid flow was investigated and compared with available flow regimes. The pressure loss along pipelines, recorded by sensors, was verified with models.

The experiment starts with the flow of gas and liquid from a CO<sub>2</sub> cylinder and water tank, respectively. The water tank is connected to a high-pressure multiphase pump that pushes water to the network pipelines. The mixing point of water and CO<sub>2</sub> occurs at the beginning of the pipeline loop. Several pressure sensors and thermocouples are fixed at specific points on the loop. In addition, gas and liquid flowmeters are installed ahead of the mixing point to record CO<sub>2</sub> and water flow rates individually. In order to read the results, all of the pressure sensors and thermocouples are connected to a data acquisition system linked to a computer.

The experimental procedure continues with the addition of fixed water velocity. The gas velocity is then increased three times towards higher velocity, with flow conditions recorded each time. The velocity of the CO<sub>2</sub> can be changed via the valve and regulator on the CO<sub>2</sub> cylinder. The next step is raising the water velocity by increasing the inlet pump pressure and changing the gas velocity several times at the same water velocity. Following this step, the velocity of the gas and liquid are altered several times and the flow type that results from the flow regime of the mixture flow is investigated. The pressure drops along the pipeline are recorded and saved on the computer.

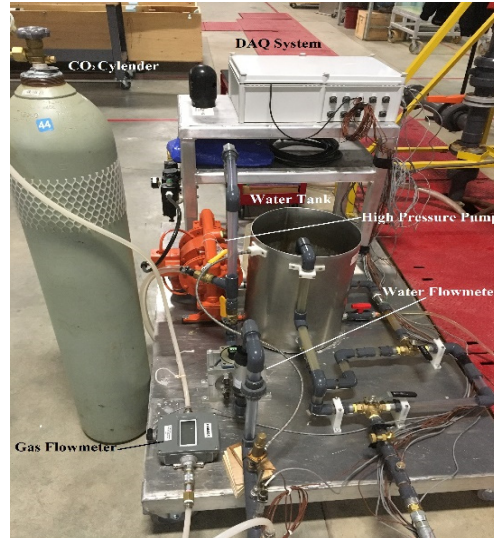


Figure 1: Experimental set-up of the fluid supply section.



Figure 2: Experimental set-up of the flow loop test section.

## 4 RESULTS AND DISCUSSION

## 4.1 Impact of water on flow pressure

When gases are flowing in a pipeline, pressure flow can be difficult to maintain. The pressure drops rapidly to less than atmospheric pressure when there is a decrease in gas flow rate and CO<sub>2</sub> gas flowing through pipes. However, by mixing water with CO<sub>2</sub> in a pipe flow, we can maintain the flow pressure and thus increase the volume of the CO<sub>2</sub> delivered.

Table 1 shows the overall flow loop pressure drop and the pressure after traveling along a 3 m length of tube versus a CO<sub>2</sub> flow rate for a single-phase flow (for CO<sub>2</sub> only). Table 2 shows the same data for a water–CO<sub>2</sub> flow.

Table 2 explains the difference in pressure values after 3 m from the starting flow on the tubing system when CO<sub>2</sub> is flowing alone and as a mixture with water. It is clear that when water flows with CO<sub>2</sub>, we can achieve a flow pressure more than 20 times higher than that of the CO<sub>2</sub> flow.

Fig. 3 also compares CO<sub>2</sub> flow and water–CO<sub>2</sub> mixture flow in terms of pressure drop for overall length of tube.

## 4.2 Phase fraction

Fig. 4 shows how phase fractions change by changing the velocities of both phases. This figure illustrates the relationship between gas phase fraction and slip ratio at different liquid flow rates. The slip ratio increases when the gas fraction increases and the flow rate of gas increases. We can also see that the velocity of water does not have as large an impact on slip ratio as CO<sub>2</sub>. Therefore, we can say that the slip ratio is more affected by the velocity of CO<sub>2</sub> than the velocity of water.

Table 1: Experimental pressure drop and pressure for CO<sub>2</sub> flow.

Gas flow (L/S)	$\Delta P$ (kPa)	Pressure at 3 m pipe length (kPa)
5	9	11
8	10	12
9	12	15
10	14	16
11	21	24

Table 2: Experimental pressure drop and pressure for water–CO<sub>2</sub> flow.

Gas Flow (L/S)	$\Delta P$ (kPa)	Pressure at 3 m pipe length (kPa)
4	158	230
8	205	294
9	227	356
10	276	445
11	285	455



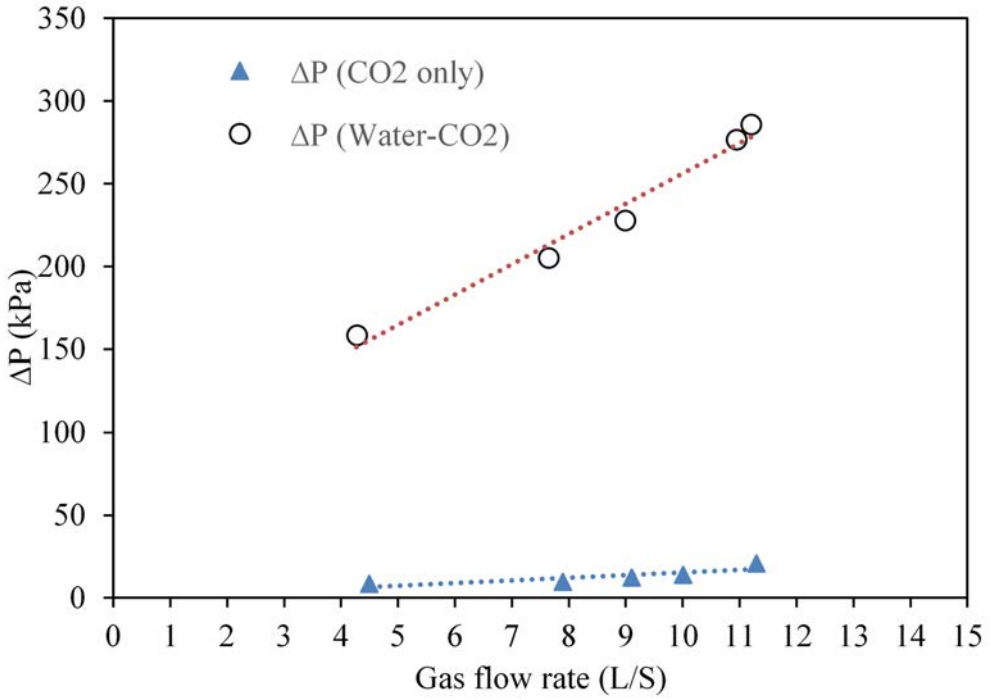


Figure 3: Comparing pressure drop vs. gas flow rate for CO<sub>2</sub> flow and water–CO<sub>2</sub> flow.

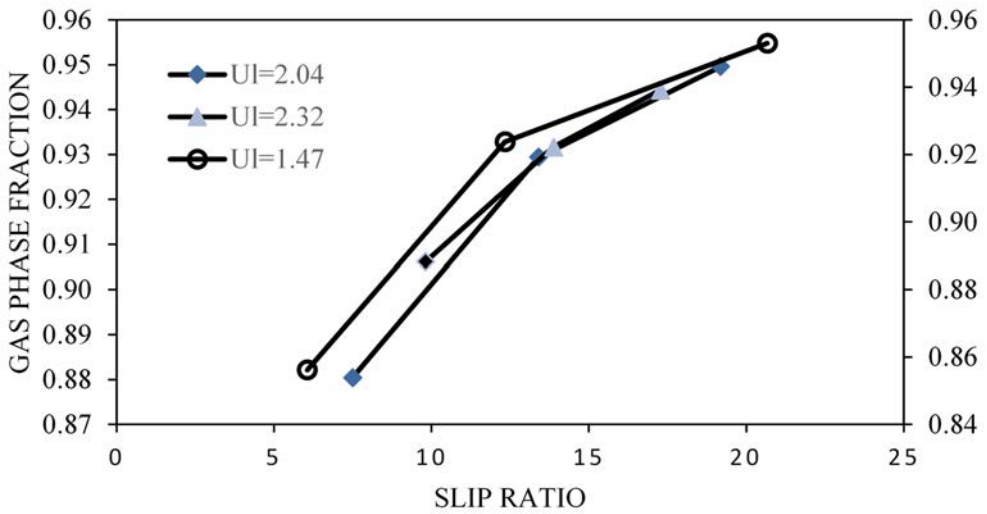


Figure 4: Relationship between slip ratio  $U_g/U_l$  and gas phase fraction for water–CO<sub>2</sub> flow.

Table 3: Slip ratio and phase fraction at different velocities of gas and liquid.

$U_L$ (m/sec)	$u_g$ (m/sec)	$S$ ( $u_g/u_l$ )	Liquid phase fraction	Gas phase fraction
1.47	8.93	6.06	0.14	0.86
1.47	18.18	12.33	0.08	0.92
1.47	30.46	20.66	0.05	0.95
2.04	15.25	7.49	0.12	0.88
2.04	27.29	13.40	0.07	0.93
2.04	39.07	19.19	0.05	0.95
2.32	22.75	9.82	0.09	0.91
2.32	32.14	13.87	0.07	0.93
2.32	40.00	17.27	0.06	0.94

### 4.3 Pressure gradient

Fig. 5 depicts experimental and theoretical overall pressure drops at different gas and liquid flow rates compared with pressure drops calculated by available correlations versus Reynold number for water  $\text{CO}_2$  flow.

According to Fig. 5, the pressure drop recorded in the experiment is nearly the same as the pressure calculated in eqn (24). Table 4 shows the percentage error between experimental and theoretical pressure drops.

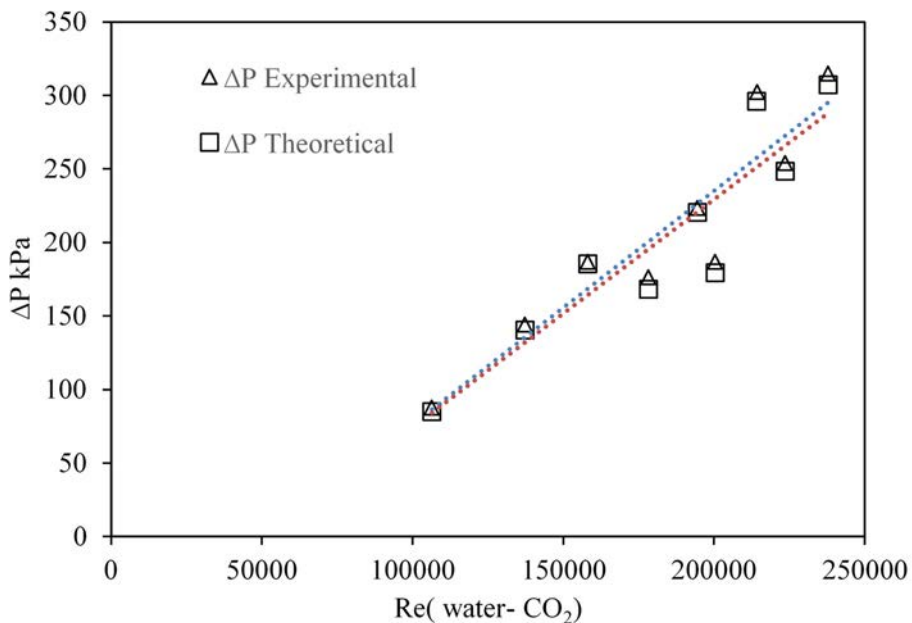


Figure 5: Pressure drop experimentally and theoretically versus Reynolds number for water- $\text{CO}_2$  flow.



Table 4: Comparison of experimental and theoretical pressure drops for water-CO<sub>2</sub> flow.

$\Delta P$ Ex kPa	$\Delta P$ Cal kPa	$\Delta P$ Error %
87.85	85.08	3.15
144.28	140.42	2.67
186.99	185.61	0.74
176.38	168.29	4.59
223.44	220.40	1.36
302.33	296.13	2.05
186.79	179.32	4.00
254.17	248.48	2.24
314.94	307.20	2.46

#### 4.4 Flow regime

The flow regime of the two-phase flow is investigated while the experiment is running. Transparent tubes are used to determine the flow type. In addition, the Beggs and Brill correlation [8] is used to estimate the flow regime of the water-CO<sub>2</sub> flow. Tables 5 and 6 show the method used to calculate the estimation of the flow regime.

As can be seen from Table 6, the flow type is always intermittent, which is the same as in the experimental system. This flow regime is confirmed for a range of CO<sub>2</sub> velocities between 8 and 40 m/sec and water velocities between 1 and 3 m/sec, flowing in a tube measuring  $\frac{3}{4}$  inches 0.01905 m in diameter.

Table 5: Reynolds and Froud Numbers for water-CO<sub>2</sub> flow vs. mixture velocity.

$U_m$ (m/s)	$Re=\rho uD/\mu$	$NFR=U_m^2/Dg$
10.40	106,600.56	24.06
19.65	137,231.00	45.46
31.94	157,994.79	73.88
17.29	159,886.96	39.99
29.32	194,318.68	67.83
41.11	214,248.56	95.09
25.07	200,396.43	57.99
34.46	223,373.01	79.71
42.32	237,282.40	97.89



Table 6: Beggs and Brill factors vs. concluded flow regime for water–CO<sub>2</sub> flow.

$\lambda_L$	$L_1$	$L_2$	$L_4$	$L_3$	NFR	Flow regime
0.14	175	0.12	111	1.71	24.06	Intermittent
0.07	144	0.55	649	4.29	45.46	Intermittent
0.04	124	1.83	2,490	8.69	73.88	Intermittent
0.11	165	0.18	186	2.23	39.99	Intermittent
0.06	141	0.67	804	4.80	67.83	Intermittent
0.04	127	1.54	2,049	7.84	95.09	Intermittent
0.09	153	0.33	364	3.17	57.99	Intermittent
0.06	139	0.72	879	5.03	79.71	Intermittent
0.05	131	1.20	1,552	6.78	97.89	Intermittent

#### 4.5 Dimensionless number trends

The values of Reynolds and Froude numbers were estimated for a range of gas and liquid velocities. As is known, the Reynolds number is the ratio of inertial forces to viscous or frictional force, while the Froude Number refers to the ratio of inertial forces to gravitational force. In Fig. 6, we attempt to determine the relationship between each number and the velocity of both phases individually.

Fig. 6 shows the relationship between pressure gradient as a function of pipeline flow distance and the Reynolds number of a two-phase flow for three values of water velocity. We can infer from the figure that the high impacts of water velocity on pressure gradients start from 2 m/s and above. These values will also result in higher Reynold's number values.

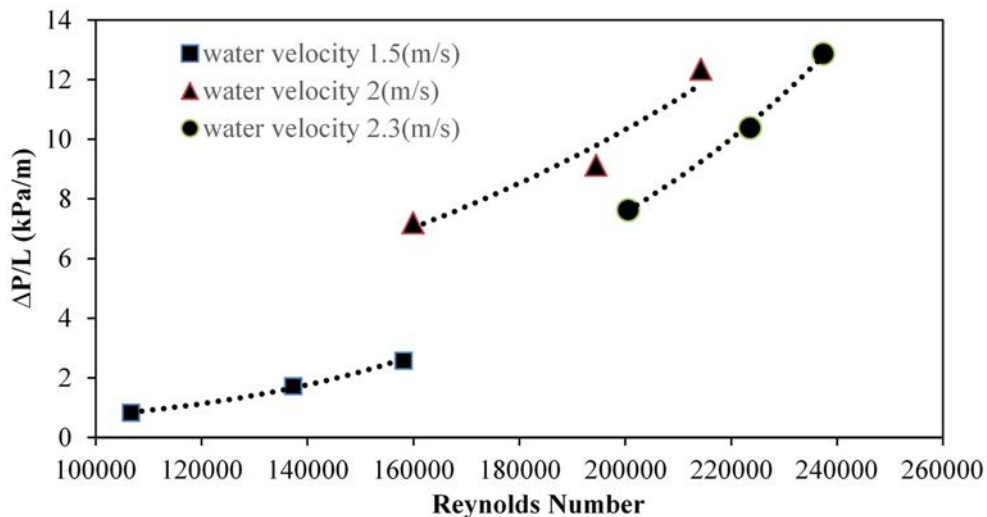


Figure 6: Pressure drop by flow distance vs. Reynold's number for three different water flow velocities.

## 5 CONCLUSION

In this work, the experimental set-up and computerization system provided real outcomes with only a small percentage of error in the permissible range. These outcomes highlight the advantage of using such a set-up for more applications pertaining to multiphase flow. The results show that there is about a 4 kPa pressure drop for each equivalent meter length of tube for water–CO<sub>2</sub> flow, while the pressure drop for water flow is about 0.4 kPa for each equivalent meter length of tube. This means that the pressure drop of water–CO<sub>2</sub> flow is approximately 10 times the pressure drop of water flow in the same tube diameter. This estimation can be used for future work to predict pressure drop for water–CO<sub>2</sub> flow applications. However, another value should be considered for pressure drop prediction, which is the ratio between pressure drop and pressure supply. In our results, this ratio is 0.17% for water flow and 0.91% for water–CO<sub>2</sub> flow.

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