# **Optimization design of a RC slab under impact load using DPSO-based multiple optimal solutions**

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# Abstract

This study presents an application of optimization algorithm to design of reinforced concrete (RC) slab under impact load. Firstly, a novel stochastic search algorithm termed discrete particle swarm optimization (DPSO) and its improvement is explained to obtain multiple optimal solutions. Then, the newly developed algorithm is applied to optimization design of RC slab under impact load. In this procedure, FE analysis is employed to evaluate the dynamic behavior of RC slab. As a result, possibility and reliability of optimization design of RC slab under impact load was demonstrated.

Keywords: discrete particle swarm optimization, RC slab, impact load.

# 1 Introduction

In order to design structures which can resist impact/impulsive load, it is necessary to investigate the index for structural safety. Especially in case an impact resistance performance is examined by using numerical analysis, it is necessary to make sure the influence of analytical parameters on results. However, it is extremely difficult to carry out these procedures because impact/impulsive behavior of concrete structures are very complicated. In practical structural optimization design, the genetic algorithms (GAs) [1], as powerful and applicable stochastic search and optimization algorithms, are finding increasing use for solving combinatorial problem.



This study presents an attempt to apply optimization algorithm to design of reinforced concrete (RC) slab under impact load. Firstly, a novel stochastic search algorithm termed discrete particle swarm optimization (DPSO) and its improvement is explained to obtain multiple optimal solutions. Then, the newly developed algorithm is applied to optimization design of RC slab under impact load. FE analysis is employed to evaluate the dynamic behavior of RC slab. As a result, possibility and reliability of optimization design of RC slab under impact load was demonstrated.

# 2 Outline of discrete particle swarm optimization algorithm

Particle swarm optimization (PSO) is a population based stochastic optimization technique developed by James Kennedy and Russel Eberhart [2] in 1995, inspired by social behavior of bird flocking or fish schooling. In PSO, solutions are called as particles, and particles have information of position (searching points) and velocity which direct the flying of the particles. Each particle has information of the previous best position, called "*pBest*<sub>i</sub>". The particle swarm optimizer tracked the best value, obtained so far by any particle in the swarm. The best value "*gBest*" is a global best solution in swarm.



Figure 1: Outline of moving particles.

PSO method searches the solution based on current position, *pBest<sub>i</sub>* and *gBest* through the problem space. Particle position is updated by summing vector values as shown in fig. 1. Here,  $x_1^k$  and  $x_2^k$  represent information of position of search point,  $v_1^k$  and  $v_2^k$  represent particle velocities, superscript *k* represents the number of iteration, *w* represents inertia weight,  $c_1$  and  $c_2$  represent learning coefficient,  $r_1$ ,  $r_2$  represent uniform random number between [0,1]. Take  $x_1^{k+1}$  for example,  $x_1^{k+1}$  is represented by linear combination of  $(v_1^k)$ ,  $(gBest - x_1^k)$  and  $(pBest_1 - x_1^k)$ .  $(v_1^k)$  means previous velocity of particle1.  $(gBest - x_1^k)$ 

means the global search, which directs the best solution in swarm.  $(pBest_1 - x_1^k)$  indicates to direct the own particle best solution in each particle, which is practically a local search procedure. Generally velocity of *i*-th particle in (k+1)-th step is calculated in the form as.

$$v_{i}^{k+1} = wv_{i}^{k} + \frac{r_{1}c_{1}(pBest_{i} - x_{i}^{k})}{\Delta t} + \frac{r_{2}c_{2}(gBest - x_{i}^{k})}{\Delta t}$$
(1)

Position of search point is calculated by

$$x_i^{k+1} = x_i^k + v_i^{k+1} \Delta t \tag{2}$$

Ordinary PSO algorithm provides only one optimal solution. In view of practical structural design, provision of possible multiple suboptimal solutions is desirable. In this study, discrete type of PSO (DPSO) [3] is used and improved by adopting ecological logic below to provide multiple suboptimal solutions.

· Conserve species of dominance

Species of dominance is most dominance in the particles. When similar particles exist, the particle is conserved as a species of dominance.

Havoc

A havoc indicates unexpected change of environment of habitat, for example, typhoon, forest fire, flood, etc.. If a havoc happened, species of dominance is supposed to decrease suddenly. Havoc also results in a mitigation of competition among species and degree of diversity of particles comes to be higher.

Turnover of species

A turnover of species means movement of species in the habitat. If current species is identified to previous species of dominance, the current species moves to other habitant.

The procedure of the improved DPSO as shown in fig. 2 is described as follows:

Step1: Initialize particle

Initial position (searching points) and velocity of each particle are generated randomly within the allowable range.

Step2: Calculate evaluation value and conserve species of dominance

The objective function value is calculated for each particle. Position of each particle is decoded as input data for numerical analysis.

Then, the affinity between particle i and j is calculated by

$$affinity_{i,j} = 1/(1 + H_{i,j})$$
(3)

where  $H_{i,i}$ =Hamming distance (i.e., similarity) between particle *i* and *j*.

The concentration  $c_i$  of particle *i* is given by

$$c_i = \sum_{j=l}^{N} a c_{i,j} / N \tag{4}$$





Figure 2: Procedure of the improved DPSO.

$$ac_{i,j} = \begin{cases} 1 & affinity_{i,j} \ge T_{affinity\_pp} \\ 0 & \text{otherwise} \end{cases}$$
(5)

Where  $T_{affinity\_pp}$  = threshold for a similarity and *N*=total number of particles. If the concentration is higher than a threshold  $T_{density}$ , the particle is conserved as species of dominance.

Step3: Set current best value of each particle as the  $pBest_i$ 

If the value is better than the current  $pBest_i$  of the particle, the  $pBest_i$  value is replaced with the current value.

If  $pBest_i$  has not been updated at a fixed interval termed *interval\_p*, N' particles selected randomly is replaced with the particles produced by uniform random number.

Step4: Set best value in the swarm as the gBest

If the best value of  $pBest_i$  is better than the current gBest, gBest is replaced with the best value and the particle number with the best value is stored.

The affinity between  $pBest_i$  and the species of dominance conserved is calculated. If this affinity is higher than threshold  $T_{affinity\_pDominanb}$  this particle is considered as same species. Next, the affinity between  $gBes_i$  and the previous species of dominance is also calculated. If this affinity is better than threshold  $T_{affinity\_gDominant}$ , this particle is replaced with a particle positioned best among low affinity particles.



Step5: Calculate particle velocity

Calculate a velocity vector for each particle by using the particle's memory and the knowledge gained by the swarm based on eqn. (1).

Step6: Update particle position

Update the position of each particle by using its velocity vector and previous position based on eqns. (6) and (7).

if 
$$\rho_i^{k+l} < \operatorname{sig}(v_i^{k+l})$$
 then  $x_i^{k+l} = 1$ ;  
else  $x_i^{k+l} = 0$  (6)  
 $\operatorname{sig}(v_i^{k+l}) = \frac{1}{2}$  (7)

$$\operatorname{sig}(v_i^{k+1}) = \frac{1}{1 + \exp(-v_i^{k+1})}$$
(7)

where,  $\rho$  is uniform random number [0,1], sig( $v_i^{k+1}$ ) is Sigmoid function.

Step7: Reach maximum iteration

If iteration number reaches the maximum iteration, then exit. Otherwise, go to Step2.



Figure 3: Reinforced concrete slab.

## 3 Application to impact resistance design of RC slab

As an example of an application of the improved DPSO algorithm to the design of a structure, an impact resistance design support system of a reinforced concrete (RC) slab under impact load is described.

The RC slab designed in this study is shown in fig. 3. It is 132 cm wide and 132 cm long square RC slab with double reinforcement. The slab thickness is a design variable. The RC slab is supported on both sides with a span length of 120 cm.

RC slabs subjected to impact load need to be designed to resist great impact through an effective combination of parameters such as the type and slab thickness of concrete, the type, number, and diameter of the reinforcing bars. For evaluating impact resistance, the results of the analysis of an impact induced failure using a dynamic nonlinear finite element method (FEM) are used as such analysis has been made possible owing to the recent advancement of numerical



analysis method. Since a dynamic nonlinear analysis requires much computation time, and a large number of design parameters are involved, a computation for all combinations of parameters for examining design alternatives is impracticable. Therefore application of the improved DPSO algorithm is suggested to present design alternatives.

#### 3.1 Outline of multilayer finite element analysis [4]

In this study, multilayer FEM model as shown in fig. 4 is used for analyzing the behavior of a RC slab subjected to an impact load. This method enables an elastoplastic analysis by vertically dividing the RC slab into several layers, applying a bending finite element analysis of a thin layer to each layer, and using a multilayer analysis. In this study, only a quarter of the RC slab is analyzed in view of the symmetry of this slab as shown in fig. 5.



Figure 4: Multilayer finite element model.



Figure 5: Analysis model (quater portion).

Prior to design simulation, a numerical simulation of impact test was conducted in order to examine an accuracy of the multilayer FEM. The impact test was carried out using pendulum type apparatus as shown in fig. 6. In this test, several types of concrete and reinforcing bar were used. The RC slab specimen is the 132 cm wide and 132 cm long square with double reinforcement. As an example of numerical simulation, calculation of the RC slab having

normal strength concrete and ordinary reinforcing bar was performed. Comparison of relation between impact force and displacement at the center of specimen is shown in fig. 7. As is obvious from this figure, both curves show good agreement in terms of the feature of load histories such as maximum impact load and softening behavior.



Figure 6: Outline of test.



Figure 7: Results of analysis.

#### 3.2 Material model and impact load in design simulation

The types of concrete used in design simulation are normal strength concrete, high strength concrete and steel fiber mixed concrete as shown in fig. 8. The types of reinforcement are ordinary bar, high strength bars, type A FRP and type B FRP bar. Only one layer of reinforcement is set at upper and lower side. Impact load used in analysis is idealized as triangular pulse as shown in fig. 9. The rate of loading is set to 500k N/ms.

#### 3.3 Evaluating indexes

In this study, three indexes below are employed to evaluate the impact performance of RC slab. These indexes are obtained by FEM analysis.



Figure 8:

Stress strain curve for concrete.

# Figure 9:

Idealized impact load.

#### 3.3.1 Impact load at a failure $P_f$

According to test results, the larger the impact load at a failure, the smaller failure is. That is, a sound structure shows higher impact load. The higher the impact load at a failure, the higher load bearing capacity the structure has.

#### 3.3.2 Local deformation index I<sub>L</sub>

The local deformation index below is proposed by Miyamoto et al. [4].

$$I_L = \frac{\phi}{\delta_u} \tag{8}$$

where,  $\phi$  is a curvature, and  $\delta_u$  is a displacement of the point of loading.

The local deformation index is calculated based on the displacement of the slab obtained by finite element analysis. This value has a close correlation with the failure mode. If the local deformation is smaller, the value of index is smaller and failure mode shows a bending.

#### 3.3.3 Impact resistance evaluation function I<sub>imp</sub>

In order to evaluate the impact resistant performance of RC slab, an impact resistance evaluation function  $I_{imp}$  was proposed by Emoto et al. [5] using local deformation index  $I_L$  and the impact load at a failure  $P_f$  is used as follows:

$$I_{imp} = \frac{P_f}{I_L} \tag{9}$$

A RC slab has higher performance to resist impact with larger value of the impact resistance evaluation function.



Parameter	type	Code
	11.05	00
Slab thickness	11.70	01
Stab unekness	12.35	10
	13.00	11
	Normal strength	00
Concrete	High strength	01
	Steel fiber mixed	10
	Ordinary	00
Reinforcement	High strength	01
Kennorcement	Type A FRP	10
	Type B FRP	11
	D13	010
	D16	011
Diameter of rehar	D19	100
Diameter of feod	D22	101
	D25	110
	D29	111
	4	001
Number of rebar	6	011
Number of feba	8	101
	10	111

Table 1:List of properties and codes for RC slabs.



Figure 10: Example of coding.

### 3.4 Coding and constraint condition

In order to combine an FE analysis with the improved DPSO, the properties of a RC slab need to be expressed in binary codes. The properties of the RC slab here mean the elements constituting the slab such as the type, the quantity and the diameter of reinforcing bars, and type and the thickness of the concrete. Since the code of each element is set at a power of two as much as possible



because a binary system is used. The coding of properties of the RC slab is listed in table 1. An example of coding is shown in fig. 10. The number of possible combinations was 110,592. In order to verify the result of design simulation, all combinations of parameters were calculated before design simulation. Constraint condition is that maximum weight of the RC slab is 5.4 kN (540 kg).

### 3.5 Design simulation

Here, design simulations are carried out for three indexes described above. In a calculation of the improved DPSO, the number of particle is set to 15, and the threshold are set to  $T_{density} = 0.45$ ,  $T_{density pp} = 0.80$ ,  $T_{affinity pDominant} = 0.80$ ,  $T_{affinity \ gDominant} = 0.125$ , interval p = 5 and interval g = 10.

### 3.5.1 Optimization design by impact load at a failure

Objective function:

To design a RC slab with a higher value of an impact load at a failure

Ten best design plans calculated beforehand are shown in table 2. The RC slab models in the shaded boxes (italicized) indicate the design alternatives obtained by the improved DPSO using the impact load at a failure as evaluating index. In this table, the impact loads obtained by FE analysis in first through fifth design plans are same values of 1,375,000 N. The improved DPSO provides three design alternatives among them and ninth design alternative. This result means that multiple solutions exist in this problem, and the improved DPSO could provide practical multiple design plans usefully.

A common feature of these plans is rich reinforcement in upper part. This may be caused because the impact load is getting larger when stiffness of surface of structure is high.

### 3.5.2 Optimization design by local deformation index

#### *Objective function:*

To design a RC slab with a smaller value of a local deformation index

Ten best design plans calculated beforehand are shown in table 3. The RC slab models in the shaded boxes (italicized) indicate the design alternatives obtained by the improved DPSO using the local deformation index. In this table, the local deformation indexes in first and second design plans are same value of  $0.1547 \times 10^{-2}$  /cm<sup>2</sup>. The improved DPSO provides first through fourth and eighth best design alternatives.

A common feature of these plans is rich reinforcement in lower part. In this case, objective function suggests that bending mode is desirable. This demand results in rich reinforcement in lower part to yield ductile tensile failure before brittle compressive failure of concrete in upper part.

#### 3.5.3 Optimization design by impact resistance evaluation function **Objective function:**

To design a RC slab with a higher value of an impact resistance evaluation function.



Table 2:Design plans by impact load at a failure.

Immost load	IIIIpact Ioau (N)	1375000		1375000		1375000		1375000		1375000		1350000		1350000		1350000		1350000		1350000	
wer part	type	Type A	FRP	Type B	FRP	Type A	FRP	Type $B$	FRP	Type $B$	FRP	Type A	FRP	Type A	FRP	Type B	FRP	Type A	FRP	Type B	FRP
cement in the lo	number of main rebar	12		12		8		8		8		12		8		8		8		12	
Reinford	Diameter	D13		D13		D13		D13		D13		D13		D19		D22		D13		D16	
per part	type	Type A	FRP	Type B	FRP	Type $A$	FRP	Type $A$	FRP	Type B	FRP	Type $B$	FRP	Type B	FRP	Type B	FRP	Type B	FRP	Type A	FRP
cement in the up	number of main rebar	16		8		16		20		20		12		16		16		20		12	
Reinford	Diameter	61Q		D25		D25		D25		D25		D13		D16		D16		D22		D25	
	Concrete	High	strength	High	strength	High	strength	High	strength	High	strength	High	strength	High	strength	high	strength	High	strength	High	strength
Slab	thickness (cm)	12.35		12.35		12.35		12.35		12.35		12.35		12.35		12.35		12.35		12.35	
Dacion	Plan	1		2		3		+		5		9		7		8		9		10	





Table 3:Design plans by the local deformation index.

Local	Deformation Index (10 <sup>-2</sup> /cm <sup>2</sup> )	0.1547	0 1547	1101.0	0.1550		0.1552		0.1552		0.1553		0.1553		0.1553		0.1555		0.1555	
wer part	type	Type A	TND0 4	FRP	Type $A$	FRP	Type B	FRP	Type B	FRP	Type B	FRP	Type B	FRP	Type $B$	FRP	Type A	FRP	Type A	FRP
ement in the lo	number of main rebar	20	20	0.4	20		20		20		20		20		20		20		20	
Reinforc	Diameter	D29		D29	D25		D20	177)	000	177)	000	670	000	D27	020	N27	D20	670	D20	<b>U</b> 4)
oper part	type	Type A	Thing R	FRP	Type $B$	FRP	Type $A$	FRP	Type $B$	FRP	Ordinoni		High	strength	Type $A$	FRP	Ordinary	UIUIIIAI y	High	strength
cement in the up	number of main rebar	20	20	0.4	8		8		8		8		8		12		8		8	
Reinford	Diameter	D13	D13	C17	D13		D13		D13		D13		D13		D13		D13		D13	
	Concrete	High	strength Hiah	strength	High	strength	High	strength	High	strength	High	strength	High	strength	High	strength	High	strength	High	strength
Slab	thickness (cm)	12.35	12 35	00.41	12.35		12.35		12.35		12.35		12.35		12.35		12.35		12.35	
	Design Plan	I	6	1	3		4		5		9		7		8		6		10	

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Table 4:

Impact	resistance evaluation function	8128834	8121019	8064516	8023107	7987220	7987220	7987220	7981928	7915947	7888698
wer part	type	Type B FRP	Type B FRP	Type A FRP	Type B FRP	Type A FRP	Type B FRP				
ement in the lo	number of main rebar	20	16	20	20	16	16	16	12	12	12
Reinforc	Diameter	D16	D29	D25	D25	D29	D29	D29	D22	D13	D13
per part	type	Type B FRP	Type A FRP	Type B FRP	Type A FRP	Ordinary	High strength	Type A FRP	Type B FRP	Type A FRP	Type B FRP
cement in the up	number of main rebar	8	16	8	8	8	8	8	20	16	8
Reinford	Diameter	D22	DI3	DI3	DI6	D13	D13	D13	D19	D19	D25
	Concrete	High streneth	High strength								
Slab	thickness (cm)	12.35	12.35	12.35	12.35	12.35	12.35	12.35	12.35	12.35	12.35
	Design Plan	Ι	2	3	4	5	9	7	8	6	10

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Figure 11: First and second design plans.

Ten best design plans are shown in table 4. The RC slab models in the shaded boxes (italicized) indicate the design alternatives. As is obvious table 4, the improved DPSO provided first through fourth best fitting design alternatives. First and second design plans are shown in fig. 11. The impact resistance evaluation function is an index combined impact load at a failure and a local deformation index, and represents an amount of energy absorption. Thus, these RC slabs have large capacity for impact in term of energy absorption.

These design simulations demonstrated that useful multiple design alternatives were provided by combining the improved DPSO with finite element method.

# 4 Conclusions

In this study, PSO algorithm was applied to the optimal design of RC slab under impact load. In order to provide multiple solutions, discrete type of PSO was improved adopting ecological logic. Then, some design simulations were performed using the improved DPSO. The conclusions of this study are summarized below:

- (1) DPSO was improved by adopting ecological logic to provide multiple design alternatives.
- (2) It was confirmed that combination of the improved DPSO and multilayer finite element method enables impact resistance design for a RC slab with highly accuracy.
- (3) Useful design plans were provided by using the three evaluating indexes. Degree of freedom in design simulation is higher by setting appropriate index for actual purpose.

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