# CALIBRATION OF THE FRACTURE LOCUS OF AN AlSi10 ALUMINUM ALLOY

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#### ABSTRACT

The aim of this paper is to calibrate the fracture locus (FL) of an aluminum alloy. The approach used is based on an iterative procedure that involves finite element (FE) simulations and experimental tests. Unidirectional tensile tests on three specimens having different notches were performed to induce different states of stress inside the material. The constitutive law was calibrated using the Voce equation. Experiments were reproduced with FE simulations to extract parameters like equivalent plastic strain at fracture, triaxiality and Lode parameter, successively used for tuning the fracture locus of the considered material.

Keywords: FEM, ductile damage models, fracture locus, Rice and Tracey, AlSi10.

### **1 INTRODUCTION**

Aluminum alloys are widely used in various engineering fields, e.g. aerospace, automotive and railway sectors. They are obtained combining Al with other constituents like Cu, Zn, Mg, Si and Mn, and are characterized by low density, high ductility and good resistance to corrosion.

Mechanical components are mostly designed to operate within the elastic field. However, in some specific sectors, e.g. crashing and impacts, it is important to also know the plastic behaviour of materials. Yielding criteria cannot be used for predicting failure, and therefore other approaches taking into account also the plastic deformations must be used to describe the fracture locus (FL) of materials.

The present work is aimed to present an experimental and numerical characterization of AlSi10Mg alloy. Several tensile tests were carried out on samples having different geometries, namely different stress states. The results of the tests were used to identify the constitutive law of the material and to calibrate a ductile damage model capable to predict the failure also in presence of high plastic deformations.

The stress state inside the material can be described by means of the stress tensor. While for the simplest model, the Maximum Strain one, the material fails when the accumulated equivalent plastic strain reaches a critical value, other more advanced formulations related the ductile damage to the stress state. Specifically, one of the most used parameter for describing the stress state is the triaxiality, namely the first stress invariant normalized by the von Mises equivalent stress. It decreases the failure strain of ductile materials exponentially (Rice and Tracey [1], Mackenzie et al. [2], Johnson and Cook [3]). Concli and Maccioni [4] calibrated the fracture locus of a weathering steel (CORTEN) using the Johnson-Cook model. Concli and Gilioli used the fracture locus of an A357 Aluminum alloy [5], [6] and of an 18-Ni300 steel [7] to assess the failure mechanisms of reticular structures produced via Selective Laser Melting (SLM). Bao and Wierzbicki [8] and Wierzbicki et al. [9] demonstrated that the different ranges of triaxiality are associated to different failure mechanisms. Barsoum et al. [10], Graham et al. [11] calibrated ductile damages models for different levels of triaxiality. Papasidero et al. [12] performed non-proportional load tests concluding that a linear model is not suitable for the description of these load conditions. Cortese et al. [13], [14] proposed a non-linear model that considers non proportional loads.



The Lode parameter, alias the third deviatoric invariant exploited with the Lode angle, has shown evidence in the mechanisms of ductile fracture (Mae et al. [15], Xue et al. [16], Ghajar et al. [17]).

In this paper, the Rice and Tracey was calibrated for an AlSi10 alloy.

# 2 MATERIAL AND METHODS

Experimental tests were performed on an MTS Criterion 45 machine owned by the Free University of Bolzano/Bozen. Force-displacement curves were obtained with tensile tests on three different geometries. A first sample has a smooth cylindrical geometry, while the others show notches to induce different stress states in the material (Fig. 1). Tests were performed with a crosshead displacement velocity of 0.1 m/min to avoid excessive heat generation that can affect the mechanical properties. Tests were run up to the break of the samples.



Figure 1: Technical specifications of the tested specimens and testing machine.



The calibration of the constitutive law  $\sigma - \varepsilon$  was done by means of an experimentalnumerical procedure in which the experimental configurations were reproduced in a the opensource FE software Salome\_Meca/Code\_Aster. The constitutive law was found iteratively comparing the results of the FE simulations in terms of force-displacement (F-s) with those measured experimentally during the tensile tests. The calibration procedure bases on the representation of the constitutive law by means of the Voce equation. This is a flexible parametric equation that reduces the number of parameters to be calibrated to 4

$$\sigma_{voce} = A + B \cdot \left( 1 - e^{-C \cdot \varepsilon_{pl}} \right) + D \cdot \varepsilon_{pl},\tag{1}$$

where A is the yielding stress (directly obtained from the elaboration of the measured data) and B, C and D are the linear coefficient, the exponential coefficient and saturation coefficient to be tuned. The iterative procedure led to the curve shown is Fig. 2. The calibrated parameters are shown in Table 1.



Figure 2: True stress-strain vs Voce calibrated curve.

Table 1: Voce parameters.

C <sub>1</sub> (MPa)	C <sub>2</sub> (MPa)	C <sub>3</sub> (-)	C <sub>4</sub> (MPa)
75	90	75	70

As previously mentioned, over the years different mathematical formulations have been proposed for describing the fracture locus. There isn't a formulation that can be considered the most effective in predicting the failure. The selection of the proper one is strongly



dependent from the ductility of the material considered. For material having a low ductility, in fact, the maximum strain model is often the best performing.

The model proposed by Rice and Tracey [1] considers a monotonic decreasing relation between the equivalent plastic strain at failure ( $\varepsilon_{peeg}$ ) and the triaxiality (t).

$$\varepsilon_{peeq} = [D_1 + D_2 \cdot exp (D_3 \cdot t)], \qquad (2)$$

where the triaxiality t is defined as the ratio between the mean stress and the equivalent stress.

Johnson and Cook [3] extended this model including the strain rate  $\varepsilon_p$  and the temperature T.

$$\varepsilon_f = [D_1 + D_2 \cdot exp \ (D_3 \cdot t)] \cdot [1 + D_4 \cdot ln(\dot{\varepsilon_p})] \cdot [1 + D_5 \cdot T], \tag{3}$$

where  $D_1$ ,  $D_2$ ,  $D_3$ ,  $D_4$  and  $D_5$  are constants to be calibrated.

Further studies by Bao and Wierzbicki [8], Wierzbicki et al. [9] and Gilioli et al. [18] showed that different levels of triaxiality are associated to different failure mechanisms. In particular, failure is due to shearing for negative values of triaxiality and to void formation mechanism for high positive values of triaxiality. In between, fracture originates due to a combination of the previous mechanisms (Fig. 3).



Figure 3: Influence of stress triaxiality on the equivalent strain to fracture [4].

Xue and Wierzbicki [19] proposed a damage model in which fracture occurs when a function depending on the equivalent plastic strain, the triaxiality and the Lode parameter becomes equal to one

$$\int_{0}^{\varepsilon_{f}} \frac{d\varepsilon}{F(t,\xi)} = 1,$$
(4)

where  $\xi$  is the Lode parameter defined as

$$\xi = \frac{27}{2} \frac{J_3}{\sigma_{\nu M}^3},$$
(5)

where  $J_3$  is the third invariant of the deviatoric stress tensor and  $\sigma_{vM}$  is the equivalent Von Mises stress.

This research focuses on high levels of triaxiality. The corresponding fracture locus is therefore calibrated according to the Rice and Tracey model (decreasing exponential function).

### **3 RESULTS**

All the tested configurations were reproduced numerically with the open-source software Salome\_Meca/Code\_Aster [20]. Two specimens were modelled taking advantage of their axis-symmetry with 2D elements while the third was modelled with 3D elements. The simulations are intrinsically non-linear due to the plastic deformations. The displacement corresponding experimentally to the failure was imposed in the FE model: the equivalent plastic strain and the triaxiality were extracted from the numerical simulations (Figs 4–6).



Figure 4: Equivalent plastic strain at fracture and triaxiality, sample #1.



Figure 5: Equivalent plastic strain at fracture and triaxiality, sample #2.



Figure 6: Equivalent plastic strain at fracture and triaxiality, sample #3.

The data extracted from the numerical analysis, namely the combination of equivalent plastic strain and triaxiality used to calibrate the fracture locus, are summarized in Table 2.

The calibrated fracture locus results from the interpolation of the three point with the least-squares method and is shown in Fig. 7.

Table 2: Parameters for the calibration of the fracture locus.

Specimen	$\varepsilon_{peeq}$	t	ξ
#1	0.087	0.39	1
#2	0.059	0.59	1
#3	0.055	0.70	0



Figure 7: Fracture locus of the considered material.

## 4 CONCLUSIONS

In this paper, by means of a procedure that relies on both experimental tests and numerical analysis, the constitutive law of an AlSi10 alloy was fine-tuned.

Moreover, the Rice and Tracey ductile damage model has been calibrated. The effects of the strain rate and of the temperature have been neglected but will be included in future studies.

Further experimental measurements on different geometries are planned to also include the effect of the Lode parameter in the calibration of the fracture locus.

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