

Effect estimation of stem density and LAI on the evapotranspiration rate from forest stand

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Abstract

The estimation model was constructed to estimate the evapotranspiration and canopy interception from the forest stand using the parameters showing the forest structure such as stem density, tree height and leaf area index. This model is expected to have the ability to estimate the effect of forest management such as stem thinning and leaf amount control. Comparing the calculated rate by this model and the observed rate in previous studies, the model can estimate the evapotranspiration and canopy interception. The effect of air temperature rise on the potential water resources was also estimated. Its decrease ratio was calculated to be around 11–13%.

Keywords: Penman–Monteith equation, roughness length, zero plane replacement.

1 Introduction

It has been one of the major topic in Japan to adapt the forest management such as stem thinning or leaf amount control for purpose of water resource management. It is said for strong dry season does not exist in Japan on the other hand, soil drought is usually not the limitation of transpiration in Japan. When soil drought limitation of the transpiration is not recognized, the amount of potential water resources defined to be annual precipitation minus annual evapotranspiration is used as the index of water resources for any forest stands (e.g. Sawano [1]). In this strategy, the estimation of evapotranspiration rate is very important to estimate the amount of potential water resources. Moreover, it is necessary to estimate the evapotranspiration using the parameters showing the forest structure such as stem density, tree height and leaf area index. If so, we



can estimate the amount potential water resources for each forest stand, or predict the effect of forest management on the amount of water resources.

Some methods are proposed to estimate the evapotranspiration rate from the forest stands using the forest micro meteorological data (e.g. Monteith [2], Shuttleworth and Calder [3]). However, most of them do not use the parameters showing the forest structure such as stem density, tree height and leaf area index. Thus, it is difficult to estimate the changes of evapotranspiration rate by forest managements, such as stem thinning or leaf amount control in direct.

Among the parameters using in Penman–Monteith equation (Monteith [2]), roughness length and zero plane replacement show the exchange efficiency of vapor between forest canopy and atmosphere, and surface conductance shows the stomata openness. Nakai *et al.* [4] reported the dependency of roughness length and zero plane replacement on stem density and tree height. Moreover, Stewart [5] proposed the equation to estimate the surface conductance that surface conductance and leaf area index are in the proportional relation. As the feature of evapotranspiration phenomenon from forest stands, canopy interception process to evaporate the intercepted rain water from the canopy surface to the atmosphere is important (Mulder [6]). The calculated values with Penman–Monteith equation means the canopy interception when g_c is fixed to be infinity. Moreover, Teklehaimanot *et al.* [7] reported the equation to show the relation between canopy interception rate and stem density.

In this paper, the estimation model for evapotranspiration rate is constructed using the parameters of stem density, tree height and leaf are index, by connecting the previous studies. The constructed model can predict the change of evapotranspiration and potential water resources by forest management such as stem thinning and leaf amount control.

2 Model

Evapotranspiration is consisted with transpiration and canopy interception loss. When canopy is dry, trees transpire through stomata. When canopy is wet with rain, water evaporates from the canopy surface to the atmosphere.

2.1 Transpiration

Transpiration rate was calculated using the Penman–Monteith equation as eqn (1) proposed by Monteith [2]:

$$IE = \frac{\Delta R_e + \rho C_p \delta q g_a}{\Delta + \gamma \left(1 + \frac{g_a}{g_c}\right)} \quad (1)$$

where IE is the transpiration rate, R_e is the effective radiation, g_c is the surface conductance, g_a is the aerodynamic conductance, ρ is the air density, δq is the vapor pressure deficit, C_p is the specific heat of air at constant pressure, and Δ is the slope of the saturation vapor pressure at air temperature, γ is the psychrometric constant.

The value of g_a was obtained from eqn (2):

$$g_a = \frac{\kappa^2 u(z)}{\left(\ln \frac{z-d}{z_0} \right)^2} \quad (2)$$

where $u(z)$ is the wind speed, z is the wind speed observation height, d is the zero plane replacement, z_0 is roughness length, and κ is the von Karman constant.

Eqns (3) and (4) is the approximation formula showing the dependency of z_0 and d , respectively, on stem density (d_s ; stem ha^{-1}) and tree height (h ; m), derived from the figures in Nakai *et al.* [4].

$$\frac{z_0}{h} = 0.2007 \exp(-0.0003d_s - 0.0001) \quad (3)$$

$$\frac{d}{h} = 0.2327 \ln(d_s) - 1.1859 \quad (4)$$

Stewart [5] proposed the eqn (5) as following for surface conductance:

$$g_c = \alpha \text{LAI} f(S) f(\delta q) f(T) f(\delta \theta) \quad (5)$$

where LAI is the leaf area index, S is the solar radiation, T is the air temperature, $\delta \theta$ is the soil moisture deficit, and f represents the functions of each of the environmental variables; α is a constant.

$f(S)$, $f(\delta q)$ and $f(T)$ are used as eqns (6)–(8), respectively, proposed by Komatsu [8].

$$f(S) = \frac{1180S}{1000 + 180S} \quad (6)$$

$$f(\delta q) = \frac{\text{EXP}(-0.569\delta q)}{\text{EXP}(-0.569)} \quad (7)$$

$$f(T) = \frac{39(T-5)}{25(T+9)} \quad (8)$$

The unit of S , δq and T in these equations are $W m^{-2}$, kPa and $^{\circ}C$, respectively.

As strong dry season does not exist in Japan, soil drought is usually not the limitation of transpiration in Japan. Thus, $f(\delta \theta)$ is fixed to be 1 in this paper. α is also fixed to be 12.36 in this paper.

2.2 Canopy interception

The calculated rate by eqn (1) with g_c to be infinity can be regarded as canopy interception (IE_i). On the other hand, Teklehaimanot *et al.* [7] reported the relations between dens and IE_i as eqn (9).

$$IE_i = \frac{8.6 \times 0.026d_s}{8.6 + 0.026d_s} \quad (9)$$

Combined with both, potential rate of IE_i was calculated with eqn (10) in this study.



$$IE_i = \frac{\Delta(R_n - G) + \rho C_p \delta q g_a}{\Delta + \gamma} \frac{8.6 \times 0.026 d_s}{8.6 + 0.026 d_s} \quad (10)$$

However, larger water than precipitation (P) cannot be intercepted by canopy, IE_i rate was judged to be equal to P, when calculated potential rate of IE_i was larger than P in a calculation unit time.

2.3 Calculation method

The necessary data to calculation are precipitation, effective radiation, solar radiation, air temperature, vapor pressure deficit and wind speed as weather condition, and stem density, tree height and leaf area index as forest stand situation.

The model was constructed for stem density and leaf area index to be input individually, to estimate the effect by forest management such as stem thinning and leaf amount control. However, this paper focuses on the model construction and their calculation ability, not on the effect estimation of forest management. Thus the relation between stem density and leaf area index was settled as Figure 1 in this study. H is also fixed to be 12.6m in this paper. Thus evapotranspiration was defined to be the amount of vapor passing up through the 14.6m height plane from forest canopy to atmosphere.

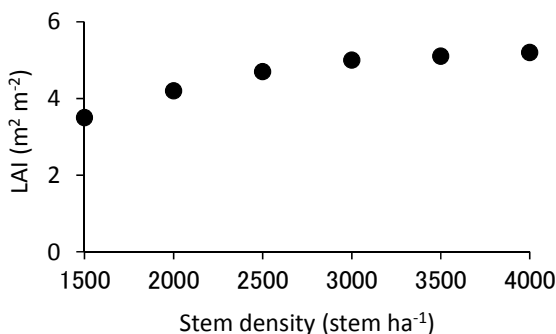


Figure 1: The values of stem density and Leaf Area Index (LAI) used in the model calculation.

3 Site description and observation method

The weather condition hourly data was observed in the Main weather station of Takaragawa Forest Watershed Experimental Station located in central Japan (36° 51' N, 139° 01' E, ASL 861m) in May–October 2011 to be no snow period. The amount of precipitation was 1,267.0 mm in this period. Figure 2 shows their monthly averaged or integrated values. The observation height of sensors are 6.5m for wind speed, 5.59m for net radiation and solar radiation, and 4.82m for air temperature and relative humidity.

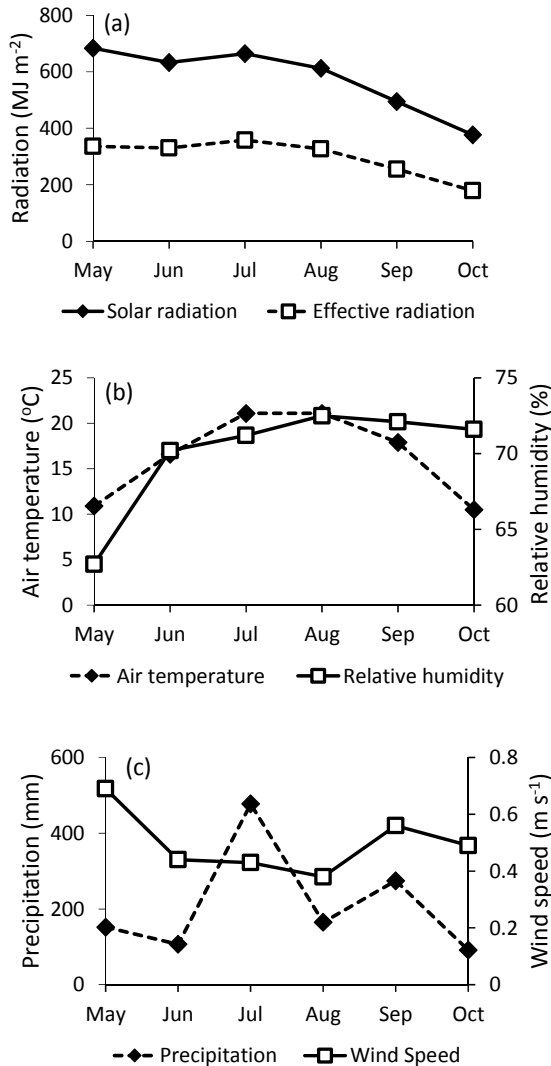


Figure 2: Average or integrate monthly weather data used in the model calculation observed in Takaragawa Forest Watershed Experimental Station in May–October, 2011. (a) Integrated monthly solar radiation and effective radiation, (b) Average monthly air temperature and relative humidity, (c) Integrate precipitation and average wind speed.

Additionally, the change of IE and potential water resources were estimated in this paper with the vertical air temperature by the global warming effect. The vertical air temperature was 4°C higher than T observed in Takaragawa in each hour. The value of relative humidity was not changed. However raised air

temperature cause to increase the value of VPD in calculation. The raised temperature to be 4°C derived from the A1F1 scenario of global warming.

4 Results and discussions

4.1 The rates of evapotranspiration and canopy interception

The evapotranspiration and rainfall interception between May and October are calculated to be 480–580mm and 210–220mm, respectively, in the range of stem density to be 1500–4000 number ha^{-1} (Figures 3 and 4). As the amount of P was 1267.0mm in this period, percentages of the IE and IE_i over P were around 38–46% and 17%, respectively. These values and percentages are compared with the previous studies derived from the observation of IE and IE_i between May and October in Japanese forest.

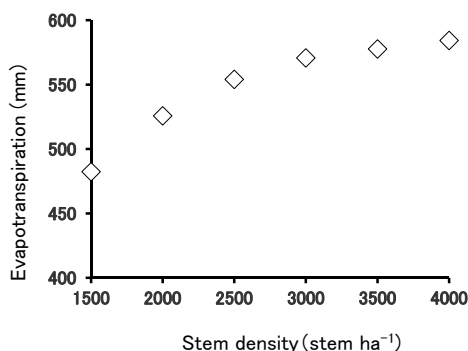


Figure 3: Calculated evapotranspiration in each stem density.

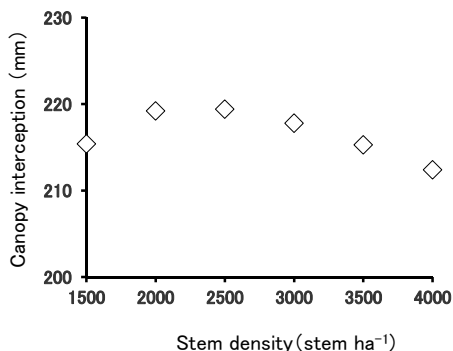


Figure 4: Calculated canopy interception in each stem density.

Kiryu Catchment (34° 58' N, 136° 0' E, ASL 190–255m, Area 5.99 ha) is covered with evergreen coniferous forest consisted with Japanese red pine (*Pinus densiflora* SIEB, et ZUCC) and Japanese cypress (*Chamaecyparis obtuse* SIEB et ZUCC). Suzuki [9] reported the rates of IE derived from the method of the short time period water budget using observed precipitation and discharge water volume from the catchment, and IE_i derived from the tank model. Tank model is consisted with tanks corresponding to canopy and stem of trees. From the balance of each tanks based on the observed P, IE_i was estimated. Summing the average monthly rates between May and October, 1972–1976 reported by Suzuki [9], IE, IE_i and P were 514.0mm, 199.2mm and 1,185.0mm, respectively. Percentages of the IE and IE_i over P were around 43% and 17%, respectively.

Yamashiro Catchment (34° 47' N, 135° 51' E, ASL 190–260m, Area 1.6 ha) is covered with secondary deciduous broad leaved forest. Most dominant species is oak (*Quercus serrata* Thunb. Ex Murray). Abe *et al.* [10] reported the monthly rates of IE derived from the method of the short time period water budget, and IE_i derived from the difference between observed P and observed precipitation on the forest floor. Summing the monthly rates between May and October, 1989 reported by Abe *et al.* [10], IE, IE_i and P were 564.0mm, 139.6mm and 1,181.0mm, respectively. Percentages of the IE and IE_i over P were around 48% and 12%, respectively.

The calculated rates by the model constructed in this paper are almost equal to those reported by Suzuki [9] and Abe *et al.* [10]. Thus it can be judged that the model have the ability to estimate the IE and IE_i properly.

4.2 Changes of evapotranspiration and canopy interception by forest management

Next, the differences of IE and IE_i among the different d_s are compared with the previous reports by Kubota *et al.* [11] and Nobuhiro *et al.* [12]. Hitach Ohta Experimental Watershed (36° 34' N, 140° 35' E, ASL 310–340m Area 0.88 ha) is covered with Japanese cedar (*Cryptomeria japonica*). The stem thinning was performed in 2009 from 2,229 stem ha^{-1} to 1,113 stem ha^{-1} . Kubota *et al.* [11] and Nobuhiro *et al.* [12] reported the changes of IE and IE_i , respectively, before and after stem thinning.

Kubota *et al.* [11] estimated IE before and after stem thinning derived from the water budget and paired catchment experiment and reported that IE after thinning was reduced to around 80% of before thinning. The calculated IE by the model were 554.0mm and 482.3mm at 2,500 stem ha^{-1} and 1,500 stem ha^{-1} , respectively. The latter is around 87% of the former. The decreased percentage calculated in the model is less than that in Kubota *et al.* [11] derived from the observation.

On the other hand, Nobuhiro *et al.* [12] reported that the percentage of through fall over the precipitation increased from 70–75% before thinning to 80–90% after thinning. Rain water reaches to a forest floor by 2 ways, through fall (pass through between the canopy) and stem flow (run down on the stem). In general, the volume of through fall is much more than stem flow. For example, Abe *et al.* [10] reported the percentages of through fall and stem flow over the

precipitation to be 80% and 7%, respectively, in Yamashiro catchment. Under the assumption that stem flow can be ignored, the report by Nobuhiro *et al.* [12] can be interpreted that the percentage of IE_i over P decreased from 25–30% before thinning to 10–20% after thinning. The calculated IE_i by the model were 219.4mm and 215.4mm at 2,500 stem ha^{-1} and 1,500 stem ha^{-1} , respectively. The percentages of IE_i over P were around 17% in both d_s , much less than that reported by Nobuhiro *et al.* [12] derived from the observation. Thus, it is judged that the model constructed in this paper has to be improved to estimate the change of canopy interception.

4.3 Effect of global warming on evapotranspiration and potential water resources

Figure 5 shows the increase rate of IE calculated by the model due to that T in Takaragawa rises $4^{\circ}C$ in observed weather data in Takaragawa. In the range of d_s to be 1,500–2,000 stem ha^{-1} , the increased rate of IE was around 72–83mm in May–October, 2011 caused that T rises $4^{\circ}C$.

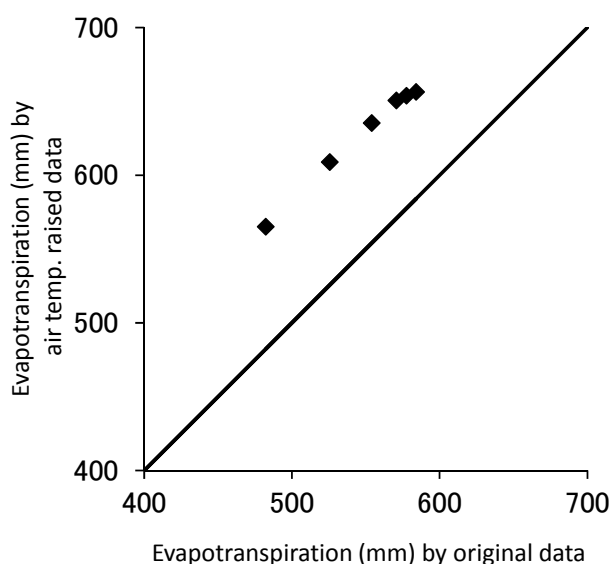


Figure 5: Comparison of evapotranspiration rate calculated with the original weather data and $4^{\circ}C$ raised air temperature data. Solid line shows that both rates are equal.

The potential water resources is defined to be the difference between P and IE . Thus the increase of IE leads the decrease of potential water resources. In the present situation using the original observed weather data in Takaragawa, potential water resources are estimated to be around 615–715mm. In case using the warming weather data that T rises $4^{\circ}C$, potential water resources decreased to

be around 540–630mm (Figure 6). The decreased ratio was calculated to be around 11–13%.

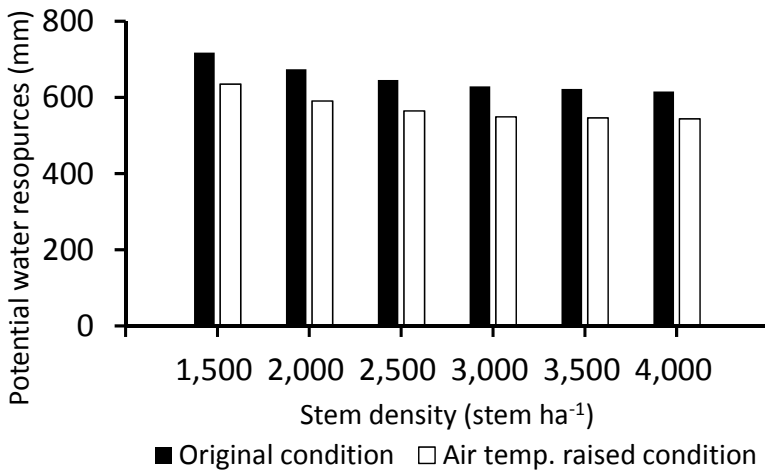


Figure 6: Comparison of potential water resources in case of original condition and raised air temperature condition.

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