

FERROFLUIDIC PLUG FLOW HEAT TRANSFER ENHANCEMENT

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ABSTRACT

Overheating of power electronic devices has become a significant issue due to their continued miniaturization and increased heat flux that needs to be dissipated. Microchannel heat sinks utilising two-phase flow are capable of very high heat transfer rates and represent a possible means of cooling such devices. In this paper, we focus on two-phase liquid–liquid plug flow using water-based ferrofluid (magnetic nanofluid) plugs as the dispersed phase and silicone oil as the continuous phase. An external magnetic field was applied to generate enhanced mixing of the microfluidic flow. We show that material properties of the ferrofluid plug influence heat transfer properties of the microfluidic flow, and demonstrate that cooling performance is further enhanced by the application of an external magnetic field, which induces mixing. We also show that microchannel heat transfer using a ferrofluid is superior to that using de-ionized water as the dispersed phase for two-phase liquid-liquid plug flow.

Keywords: electronics cooling, ferrofluid, heat transfer, magnetic field, microfluidic, two-phase

1 INTRODUCTION

Improved cooling technologies for power electronic devices are in high demand due to the desire for greater power density and the rapid expansion of photovoltaic systems. Integrated liquid cooling provides a solution to facilitate further miniaturization and increased power density of electronic devices. However, integrated liquid cooling utilises microchannels to transport fluid, and microchannel fluid flow is characterised by laminar flow at low Reynolds numbers. These characteristics make molecular diffusion the main mode of heat transfer, which is insufficient to remove heat at a rate that is required from high performance power electronic devices. Hence, to enhance heat transfer, we introduced three ‘upgrades’. The first upgrade is to improve the thermal conductivity of the working fluid. Ferrofluids are composed of small (3–15 nm) particles of solid, magnetic, single-domain particles coated with a molecular layer of a dispersant or surfactant, and suspended in a liquid carrier [1]. The percentage, size and type of magnetic nanoparticle, surfactant and dispersion medium, including the method of synthesis dictates the thermophysical properties of ferrofluids, which influences the transport properties and thus, heat transfer properties of the microfluidic flow [2–5]. Thermal agitation keeps the particles suspended because of Brownian motion, and the coatings prevent the particles from sticking to each other [1].

Due to the small size of the particles, and thus increased contact surface area for heat transfer, ferrofluids offer the ability to significantly enhance heat transfer as reflected by the higher thermal conductivity it has compared to traditional cooling liquids such as de-ionized water (DIW) [3, 6, 7]. Ferrofluids have been commonly used in audio loudspeakers to improve its audio response and exhibit better power handling. They are also used as seals for rotating shafts to almost eliminate frictional losses compared to traditional mechanical seals or high-speed computer disk drives to keep out harmful dust particles and impurities. Therefore, manufacturing technologies of commercial ferrofluids are advanced and reliable. The second upgrade is to introduce rapid mixing in the ferrofluidic flow. This can be induced within the

microchannel flow either by active or passive methods [8]. In this paper, we actively induce rapid mixing by the application of an external magnetic field using permanent magnets. The superparamagnetic nanoparticles in ferrofluids allows them to be easily manipulated by an external magnetic field, and immediately redisperses once the magnetic field is removed. The third upgrade is to adopt two-phase flow. Two-phase flow has been shown to significantly enhance heat transfer rates relative to single-phase flow by up to 500% [9–12]. Furthermore, because liquids have higher thermal conductivity than gases, two-phase liquid-liquid flow has the potential to enhance heat transfer more effectively than two-phase gas-liquid flow [12]. Ferrofluid plugs and silicone oil are the dispersed and continuous phase respectively.

Combining these three upgrades provides the potential for the dissipation of ever increasing heat loads, which aids in the development of greater product reliability and performance of power electronic devices.

1.1 Two-Phase Heat Transfer

There has been no publications reporting the use of ferrofluid plugs as the dispersed phase in two-phase liquid-liquid plug flow to enhance heat transfer rates. However, there have been studies on heat transfer in two-phase liquid-liquid Taylor/slug/plug flow using silicone oil as the continuous phase, and DIW as the dispersed phase in minichannels. The fundamental concepts from these studies should be applicable to the research study with the exception of using ferrofluid plugs instead of DIW. Eain *et al.* [11] conducted experimental investigations examining potential heat transfer enhancements of a two-phase liquid-liquid Taylor flow regime. They studied the effects of slug length and carrier phase variations of Pd5, Dodecane and AR20 silicone oils on the local Nu. Enhancements up to 600% over conventional Poiseuille flow were observed in the fully-developed region. It was found that shorter carrier slugs approaching the channel diameter, and longer water slugs provided the greatest heat enhancement. Furthermore, it was also reported that slugs are able to reach thermal equilibrium faster, thus having shorter thermal entrance lengths as compared to continuous flow. Bandara [13] also conducted numerical and experimental studies on heat transfer and pressure drop on two-phase liquid-liquid slug flow using silicone oil and DIW. He reported having up to 400% enhancements in heat transfer compared to conventional Poiseuille flow. This gives confidence in enhancing heat transfer utilising two-phase liquid-liquid plug flow. It must be noted that studies by Liu *et al.* [14] and Che *et al.* [10] report that shorter plug lengths lead to higher heat transfer, which is in disagreement to Eain *et al.* [11].

2 MATERIALS AND EXPERIMENTAL METHODS

2.1 Material Characterization

2.1.1 Particle Sizing

It is well known that the size, shape and composition of the magnetic nanoparticles strongly influence the thermophysical profile of the ferrofluid, and thus, their transport and flow properties. Since all the diluted samples contain magnetite (Fe_3O_4) magnetic nanoparticles, the only variable is size. Depolarized dynamic light scattering (DDLS) and transmission electron microscopy (TEM) were employed to size the particles.

2.1.2 Transport Properties

Viscosity and thermal conductivity are important properties for designing heat dissipation devices. These properties depend on the type and concentration of magnetic nanoparticles

and surfactant make-up of the ferrofluid. The type and strength of external magnetic field applied also affects these properties.

Viscosity

Kinematic viscosity of the diluted ferrofluid samples was measured at 25°C using a capillary viscometer (Micro-Ubbelohde 531 10, SCHOTT) along with a viscosity measuring system (ViscoSystem® AVS350, SCHOTT). The viscosity measuring system records the time taken to flow past two points in the capillary viscometer. This measurement was taken three times, and the final reading is the average of the three. DIW was used as the calibration standard.

Grade N42 neodymium permanent magnets (40 x 15 x 8 mm, Aussie Magnets) were used to apply an external magnetic field to the ferrofluid. Magnetic flux, B was varied ($0 \leq B \leq 50$ mT, $\Delta B = 10$ mT) by varying the offset distance between the capillary tube and the magnets.

Thermal Conductivity

Thermal conductivity of the ferrofluid samples were measured at 25°C using the KD2 Pro Thermal Property Analyzer (Decagon Devices Inc.), which is based on the transient hot-wire method. The KS-1 single needle sensor was used. The fluid sample was held in an aluminium box connected to a water bath (MB-5, Julabo), hence temperature of the sample was kept at a constant. Permanent magnets were used to apply an external magnetic field to the ferrofluids and magnetic flux was varied ($0 \leq B \leq 50$ mT, $\Delta B = 10$ mT) by varying the offset distance between the aluminium box and the magnets.

2.2 Dispersed Phase

2.2.1 Commercial Ferrofluid

The domain detection kit consisting of EMG308, EMG408, EMG707, EMG708 and EMG807 (Domain Detection Kit, Ferrotec) ferrofluid samples were used for single-phase flow heat transfer experiments. The samples were then diluted with DIW to make diluted samples of 5% and 10% ferrofluid content with DIW (refer to Table 1).

For two-phase flow experiments, only EMG707 (Ferrotec) was used to make a diluted sample of 20% ferrofluid content with DIW. 20% dilution gives a ratio of ferrofluid:DIW as 0.2:0.8. Thermophysical properties of the diluted commercial ferrofluid sample were measured and compiled (refer to Table 1).

2.2.2 Self-Fabricated Ferrofluids

In order to have control and information on the fluid and surfactants, we also made our own water-based Fe_3O_4 ferrofluids. Different surfactants were used using the co-precipitation method, which forms polydisperse iron oxide nanoparticles [15]. To make about 3.75 g of Fe_3O_4 nanoparticles, the following material and steps were used;

1. Take 3.26 g of $\text{FeCl}_2 \cdot 4\text{H}_2\text{O}$ and 8.7 g of $\text{FeCl}_3 \cdot 6\text{H}_2\text{O}$ and dissolve in 380 mL of DIW.
2. Under vigorous stirring, slowly add 20 mL of 25% NH_3 . The pH should be about 11–12.
3. Sediment the precipitate with a very strong rare earth magnet (or centrifuge for 5 minutes at 5000 rpm) and wash until the pH drops from 10 to 7.
4. Continue to sediment and precipitate until desired volume concentration of Fe_3O_4 superparamagnetic iron oxide nanoparticles (SPIONs) is obtained.

Table 1: Measured properties of commercial diluted ferrofluid samples.

Sample	Magnetite Content (% by Volume)	Measured Properties		
		Density (kg/ m ³)	Dynamic Viscosity (mPa·s)	Thermal Conductivity (W/(m·K))
EMG308 5%	0.02–0.055	1006.0	1.025	0.646
EMG308 10%	0.04–0.11	1008.1	1.046	0.644
EMG408 5%	0.02–0.055	1004.6	1.029	0.636
EMG408 10%	0.04–0.11	1006.2	1.040	0.626
EMG707 5%	0.05–0.2	1012.9	1.078	0.642
EMG707 10%	0.1–0.4	1021.0	1.103	0.645
EMG707 20%	0.2–0.8	1022.5	1.113	0.655
EMG708 5%	0.05–0.2	1005.9	1.029	0.682
EMG708 10%	0.1–0.4	1009.8	1.060	0.684
EMG807 5%	0.05–0.4	1006.7	1.040	0.644
EMG807 10%	0.1–0.8	1009.7	1.050	0.651
DIW	-	1000.0	1.000	0.610

To determine the volume concentration of the SPIONs, a Prussian blue assay was performed. It was found that the SPIONs had a solid volume concentration of 1.5%. Before functionalizing the SPIONs, TEM was performed to check whether the SPIONs are worth functionalizing. The particle size ($d \sim 10$ nm for Fe_3O_4) and coagulation (whether the particles clumped together) were the criterion of interest.

Three different surfactants were used to functionalize the fabricated SPIONs – dopamine (DPA), tetramethylammounium hydroxide (TMAH), and citric acid. The surfactants were added drop-wise to the SPIONs while swirling at the same time. All three ferrofluid types had the same volume concentration of solid magnetic nanoparticles (~ 1.5 %) and surfactant ($\sim 10\%$). Only the ferrofluids fabricated with DPA and TMAH as surfactants remained stable. They were then diluted with DIW to 20% dilution, which gives a ratio of ferrofluid:DIW as 0.2:0.8. Thermophysical properties of the diluted samples were measured and compiled in the Table 2.

2.3 Continuous Phase

0.65 cSt silicone oil (PMX-200, Xiameter) with a thermal conductivity of 0.1 W/(m·K) was used as the continuous phase in two-phase flow heat transfer experiments.

Table 2: Measured properties of fabricated diluted ferrofluid samples

Sample	Magnetite Content (% by Volume)	Measured Properties		
		Density (kg/m ³)	Dynamic Viscosity (mPa·s)	Thermal Conduc- tivity (W/(m·K))
DPA 20%	~ 0.3	1003.5	1.014	0.630
TMAH 20%	~ 0.3	1006.2	1.037	0.686

2.4 Microchannel Fabrication

To fabricate the microchannel, we adopted the proposed method by Saggiomo and Velders [16]. The design of the sacrificial microchannel mould was first 3D printed out of acrylonitrile butadiene styrene (ABS) with a layer thickness of 0.254 mm (or 254 μm) at RMIT's Advanced Manufacturing Precinct (AMP) using the uPrint SE 3D Printer (Stratasys) (see Fig. 1). The microchannel mould undergoes vapour smoothing with acetone. Following this process, optical profiling was performed using the Olympus LEXT OLS4100 3D Measuring Laser Microscope to obtain the surface roughness measurements of the untreated and treated microchannel sacrificial moulds. Two untreated (samples 1 and 2) and two treated (samples 3 and 4) sacrificial moulds were inspected. The results show that the treated sacrificial moulds are about four times smoother compared to the untreated moulds, with an approximate roughness to channel diameter ratio of 1/100. A nichrome heater coil (wire gauge 28) was then carefully wrapped around the treated sacrificial mould at the allocated location along the straight length. Thermocouples were positioned near the microchannel with the help of access ports created using additional stems in the ABS thermocouple adapter. Degassed PDMS at a mixture ratio of 10:1 was then poured into the pre-prepared glass mould over the sacrificial mould. The PDMS is left to cure in the oven at 75°C for 2–3 hours. The thermocouple adapter and PDMS mould was removed, and the cured thermocouple-embedded microchannel PDMS is soaked in acetone for at least 48 hours to allow the acetone to soften the sacrificial mould. Acetone was then pushed through the inlet/outlet ports of the PDMS mould using a needleless syringe until all the sacrificial mould was fully dissolved and flushed out, creating a cavity. Finally, DIW is flushed through the cavity to clear any remaining solid particles, producing the desired microchannel.

2.5 Flow Visualization – Enhanced Magnetic Mixing

Fluorescein mixture – 0.05 g of fluorescein sodium salt (F6377-100G, Sigma-Aldrich) mixed with 20 mL of DIW and EMG707 20% ferrofluid (Ferrotec) were the materials used. The 3D casted mould was used as the microfluidic chip. Single-phase flow was visualized using an inverted microscope (Eclipse TS100, Nikon) and recorded using a microscopy camera (USB 2.0 Camera, Edmund Optics). Ferrofluid and fluorescein mixture were individually introduced to the microfluidic chip using a precision syringe pump (SPM 100, SIMTech Microfluidics Foundry) via a plastic syringe (10 mL luer slip, Terumo). All connection tubes were attached to the microfluidic chip using ultraviolet (UV) curing glue (3526, Loctite). A 3.2 mm³ neodymium (NdFeB) permanent magnet (B222, K&J Magnetic Inc.) was used to introduce an external magnetic field. The mixture of ferrofluid and fluorescein dye was collected at the outlet collection reservoir and properly disposed of after the experiment. The magnet was placed at two different positions – magnet position 1 and magnet position 2 (see Fig. 2), to observe any difference in mixing ability due to magnetic flux strength.

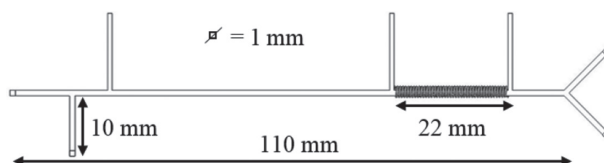


Figure 1: Microchannel sacrificial mould dimensions.

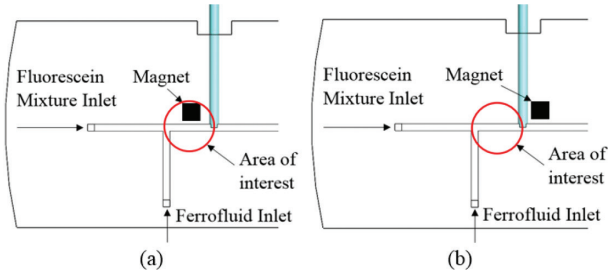


Figure 2: Enhanced magnetic mixing. (a) Magnet Position 1; (b) Magnet Position 2.

2.6 Heat Transfer

2.6.1 3D Casted Mould

Eight T-type thermocouples (Teflon-insulated twisted pair solid 1/0.2 mm diameter) were embedded in the PDMS; two thermocouples embedded into the microchannel flow – one at the inlet heated area, and the other at the outlet heated area. The other six thermocouples were along the microchannel length (see Fig. 3). Small diameter thermocouple wires were used to minimise conduction losses. Temperature was recorded using a temperature data logger (TC-08, Pico Technology). The temperature measurement system was calibrated against a traceable platinum resistance thermometer (PRT) (P795, Dostmann) in a uniform temperature water bath with an immersion circulator (MPC-E, Huber).

2.6.2 Two-Phase Flow

Three different ferrofluid samples – EMG707 20%, TMAH 20% and DPA 20% were used as the dispersed phase, while 0.65 cSt silicone oil was used as the continuous phase. Prior to recording data using ferrofluidic plugs, DIW was used as the dispersed phase to calibrate the obtained results.

2.6.3 Nusselt Number Calculation

Nusselt number, Nu , is expressed as

$$Nu = \frac{hD_h}{\kappa} \tag{1}$$

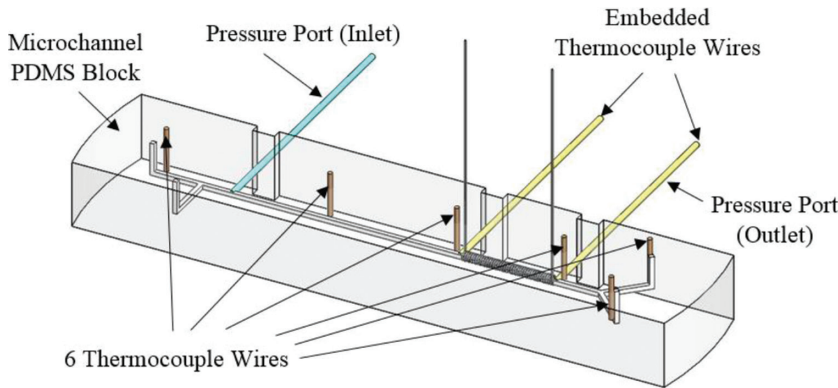


Figure 3: Embedded thermocouples in microchannel flow (Isometric View)

where D_h represents the characteristic length or hydraulic diameter in m, and κ is the thermal conductivity of the fluid in W/(m·K). The convective heat transfer coefficient of the flow, h in W/(m²·K), is expressed as

$$h = \frac{q_f}{(T_{w,avg} - T_{f,avg})} \quad (2)$$

where q_f is the heat flux in W/m², $T_{w,avg}$ is the average wall temperature difference $(T_{w,out} + T_{w,in})/2$ in K, and $T_{f,avg}$ is the average fluid temperature difference $(T_{out} + T_{in})/2$ in K. Here, q_f can be calculated as

$$q_f = \frac{Q\rho c_p (T_{out} - T_{in})}{A} \quad (3)$$

where Q is the volumetric flow rate in m³/s, ρ is density of the fluid in kg/m³, c_p is the specific heat capacity of the fluid in J/(kg·K), $(T_{out} - T_{in})$ is the average fluid temperature difference in K, and A is the area in contact with the fluid in m².

As the solid volume fraction of magnetic nanoparticles is estimated to have an average of 0.03 – 0.4 % depending on the sample, ρ and c_p for ferrofluid was assumed to have about the same value as the carrier fluid (DIW).

For the experiments, Nu was scaled in accordance with DIW, where the theoretical value of Nusselt number is 3.61 for a square cross-section microchannel.

3 RESULTS AND DISCUSSION

3.1 Material Characterization

3.1.1 Particle Sizing

The average particle size for all ferrofluid samples that were obtained performing DDLS was between 6–8 nm. The reliability of these results was verified by performing TEM on the samples, which resulted in an average particle size of 10–15 nm. The particle sizes obtained from TEM are slightly larger than those obtained from DDLS. This is due to the evaporation under ambient atmosphere of the solution during sample preparation, where the nanoparticles are deposited onto strong carbon grids (GSCu200C-50), spurring the nanoparticles towards further aggregation due to the elevating free energy at the grain boundary [5].

3.1.2 Transport Properties

It was observed that viscosity increases linearly with increase in magnetic flux strength at room temperature (RTP), and thermal conductivity increases exponentially with increase in magnetic flux strength (see Fig. 4).

3.2 Flow Visualization

3.2.1 Single-Phase Enhanced Magnetic Mixing

In the absence of a magnetic field, a 1:1 ratio of ferrofluid:fluorescein mixture needs to be achieved (see Fig. 5). Fluorescein mixture and the ferrofluid were introduced at a flow rate of 800 μ L/min and 50 μ L/min, respectively. Without a magnet, very slight mixing of the ferrofluid and fluorescein mixture occurred via molecular diffusion. However, with the application

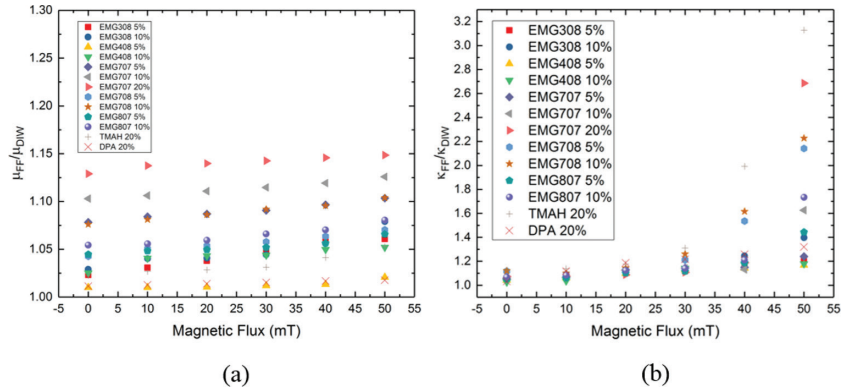


Figure 4: Transport properties of ferrofluids (with magnetic field) (a) μ_{FF}/μ_{DIW} ; (b) κ_{FF}/κ_{DIW} .

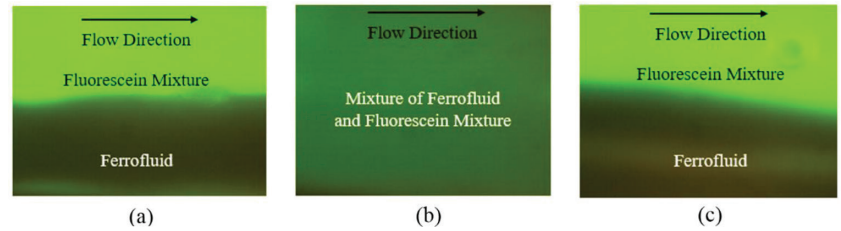


Figure 5: Single-phase flow visualization – enhanced magnetic mixing results. (a) No magnetic field; (b) Magnet position 1; (c) Magnet position 2.

of a magnetic field, it was observed that mixing was greatly enhanced. At magnet position 1 (see Fig. 2), mixing occurred rapidly as observed by the fluorescein mixture mixing with the ferrofluid and filling the entire channel (see Fig. 5). At magnet position 2, because the magnetic field is further away from the area of interest, magnetic flux applied to the area is therefore reduced (see Fig. 5). Hence, less mixing is observed. It can thus be concluded that mixing is enhanced with increased magnetic flux.

3.3 Heat Transfer

3.3.1 DIW Calibration

As a benchmark, against which to compare the heat transfer enhancement provided by the ferrofluids, the heat transfer enhancement of two-phase flow using DIW as the dispersed phase and 0.65 cSt silicone oil to single-phase DIW was measured. Results showed an approximate doubling (200%) of heat transfer of the two-phase compared to single-phase flow.

3.3.2 Single-Phase Heat Transfer Enhancement (No Magnetic Field)

EMG708 5% recorded the highest heat transfer enhancement of 116% improvement compared to DIW (see Fig. 6). This large improvement can be attributed to the induced magnetic flux of 6 mT produced by the nichrome heater coil. EMG708 10% has a higher percentage of magnetic nanoparticles, which should theoretically result in higher heat transfer rates. However, EMG708 10% records a lower Nu compared to EMG708 5%.

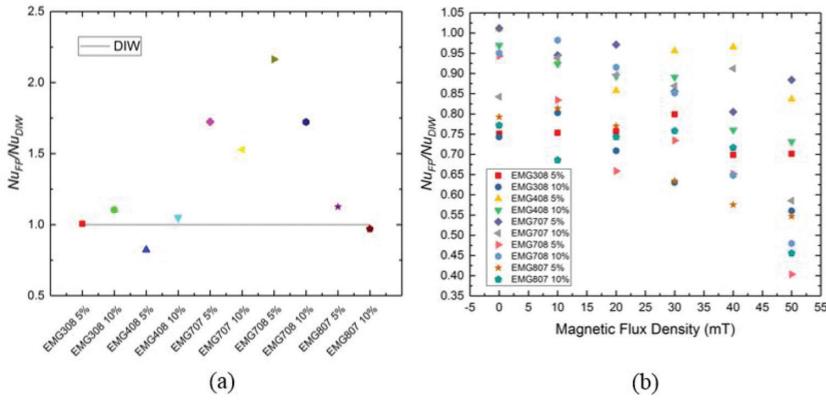


Figure 6: Single-phase flow Nu_{FF}/Nu_{DIW} Results, $Re = 11.6$. (a) No magnetic field; (b) With magnetic field.

3.3.3 Single-Phase Heat Transfer Enhancement (With Magnetic Field)

Magnetic field strengths of 10, 20, 30, 40 and 50 mT were applied to the fluid flow at the heated section. Generally, it was observed that Nu decreases with increasing magnetic field strength for all diluted ferrofluid samples (see Fig. 6). This could be attributed to the solid magnetic nanoparticles getting attracted to, and at high enough magnetic fluxes pinned in place against, the wall of the channel under the action of the magnetic field. The removal of the nanoparticles from the carrier fluid reduces the effective thermal conductivity of the mixture. This in turn is detrimental to heat transfer at the area where magnetic flux is applied and high magnetic fluxes.

3.3.4 Two-Phase Ferrofluidic Plug Flow Heat Transfer Enhancement (No Magnetic Field)

Using ferrofluid plugs as the dispersed phase, the heat transfer rate increased (at low Re) compared to using DIW as the dispersed phase (see Fig. 7). It can also be observed that commercial ferrofluid EMG707 20% yielded the highest heat transfer enhancement, followed by TMAH 20% then DPA 20% in the absence of an external magnetic field. This then shows an almost three times enhancement of heat transfer rate compared to DIW only at low Re ($Re = 2.32$).

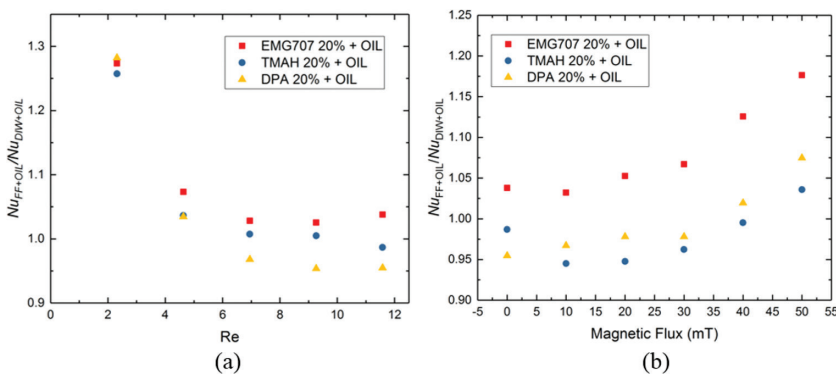


Figure 7: $Nu_{FF+OIL}/Nu_{DIW+OIL}$ Results. (a) No magnetic field; (b) With magnetic field @ $Re = 11.6$.

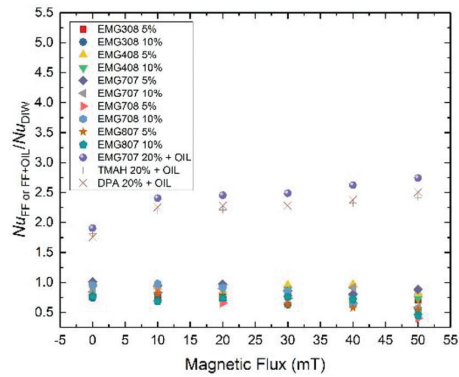


Figure 8: Comparison of Single-phase and two-phase heat transfer enhancement (with magnetic field), $Re = 11.6$

Heat transfer may only be enhanced at low Re because the plugs may have detached from the channel wall with increased flow rates. This is explained by Bandara [13] where plug length decreases in size with increased Re . We will visualize this experiment in future.

3.3.5 Two-Phase Ferrofluidic Heat Transfer Enhancement (With Magnetic Field)

Under the influence of an external magnetic field, there is improved heat transfer enhancement compared to the case when no external magnetic field was applied (see Fig. 7). It was also observed that heat transfer is enhanced with increased magnetic flux strength. This is different from single-phase flow heat transfer results previously obtained, where heat transfer rate decreases under the influence of an external magnetic field (see Fig. 8). This could be because the solid magnetic nanoparticles do not come out of solution and get stuck to the channel wall under the influence of an external magnetic field with the presence of the oil phase.

4 CONCLUSIONS AND RECOMMENDATIONS

Two-phase liquid-liquid plug flow showed higher heat transfer rates if DIW was replaced by a ferrofluid as the dispersed phase. Without an external magnetic field, heat transfer rate of ferrofluidic plug flow is about the same as when DIW is used as the dispersed phase, except at low Re . In general, two-phase liquid-liquid plug flow approximately doubles heat transfer rate compared to single-phase flow. We also observed that heat transfer rates are different for different ferrofluid types. Also, with the application of an external magnetic field, heat transfer rates for two-phase liquid-liquid plug flow were enhanced. We self-fabricated ferrofluids with the same magnetic nanoparticle type, and coated the nanoparticles with two different surfactants – dopamine (DPA) and tetramethylammonium hydroxide (TMAH). We found that in the absence of an external magnetic field, both DPA and TMAH coated ferrofluids exhibited similar heat transfer rate enhancement. However, in the presence of an external magnetic field, DPA coated ferrofluid recorded slightly higher heat transfer rate enhancement compared to TMAH coated ferrofluid. All in all, two-phase liquid-liquid plug flow using ferrofluid plugs as the dispersed phase, under an external magnetic field, yields higher heat transfer rates compared to using DIW as the dispersed phase.

Future works will include pressure drop studies comparing the increase in pressure drop (ΔP) due to two-phase liquid-liquid plug flow as opposed to single-phase flow. The aim is to maximize $Nu/\Delta P$.

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REFERENCES

- [1] Rosensweig, R.E., *Ferrohydrodynamics*, Dover edition ed. Mineola, New York: Dover Publications, Inc., 1997.
- [2] Abareshi, M., Goharshadi, E.K., Zebarjad, S.M., Fadafan, H.K. & Youssefi, A., Fabrication, characterization and measurement of thermal conductivity of Fe₃O₄ nanofluids. *Journal of Magnetism and Magnetic Materials*, **322**, pp. 3895–3901, 2010.
<https://doi.org/10.1016/j.jmmm.2010.08.016>
- [3] Alsaady, M., Fu, R., Li, B., Boukhanouf, R. & Yan, Y., Thermo-physical properties and thermo-magnetic convection of ferrofluid. *Applied Thermal Engineering*, **88**, pp. 14–21, 2015.
<https://doi.org/10.1016/j.applthermaleng.2014.09.087>
- [4] Ghasemi, E., Mirhabibi, A. & Edrissi, M., Synthesis and rheological properties of an iron oxide ferrofluid. *Journal of Magnetism and Magnetic Materials*, **320**, pp. 2635–2639, 2008.
<https://doi.org/10.1016/j.jmmm.2008.05.036>
- [5] Jiang, W. & Wang, L., Monodisperse magnetite nanofluids: Synthesis, aggregation, and thermal conductivity. *Journal of Applied Physics*, **108**, 2010.
<https://doi.org/10.1063/1.3518045>
- [6] Nkurikiyimfura, I., Wang, Y. & Pan, Z., Heat transfer enhancement by magnetic nanofluids: a review. *Renewable and Sustainable Energy Reviews*, **21**, pp. 548–561, 2013.
<https://doi.org/10.1016/j.rser.2012.12.039>
- [7] Li, Q., Xuan, Y. & Wang, J., Experimental investigations on transport properties of magnetic fluids. *Experimental Thermal and Fluid Science*, **30**, pp. 109–116, 2005.
<https://doi.org/10.1016/j.expthermflusci.2005.03.021>
- [8] Che, Z., Nguyen, N.T. & Wong, T.N., Analysis of chaotic mixing in plugs moving in meandering microchannels. *Physical Review E*, **84**, p. 066309, 2011.
<https://doi.org/10.1103/physreve.84.066309>
- [9] Nguyen, N.T. & Wereley, S.T., *Fundamentals and applications of microfluidics*, Second ed.: Artech House, 2006.
- [10] Che, Z., Wong, T.N. & Nguyen, N.-T., Heat transfer enhancement by recirculating flow within liquid plugs in microchannels. *International Journal of Heat and Mass Transfer*, **55**, pp. 1947–1956, 2012.
<https://doi.org/10.1016/j.ijheatmasstransfer.2011.11.050>
- [11] Eain, M.M.G., Egan, V. & Punch, J., Local Nusselt number enhancements in liquid-liquid Taylor flows. *International Journal of Heat and Mass Transfer*, **80**, pp. 85–97, 2014.
<https://doi.org/10.1016/j.ijheatmasstransfer.2014.09.009>
- [12] Bandara, T., Nguyen, N.-T. & Rosengarten, G., Slug flow heat transfer without phase change in microchannels: a review. *Chemical Engineering Science*, **126**, pp. 283–295, 2015.
<https://doi.org/10.1016/j.ces.2014.12.007>

- [13] Bandara, P.M.T., *Heat transfer enhancement in microchannels with liquid-liquid slug flow*. Doctor of Philosophy, RMIT University, 2015.
- [14] Liu, J., Tan, S.-H., Yap, Y.F., Ng, M.Y. & Nguyen, N.-T., Numerical and experimental investigations of the formation process of ferrofluid droplets. *Microfluidics and Nanofluidics*, **11**, pp. 177–187, 2011.
<https://doi.org/10.1007/s10404-011-0784-7>
- [15] Lu, A.-H., Salabas, E.L. & Schüth, F., Magnetic nanoparticles: synthesis, protection, functionalization, and application. *Angewandte Chemie International Edition*, **46**, pp. 1222–1244, 2007.
<https://doi.org/10.1002/anie.200602866>
- [16] Saggiomo, V. & Velders, A.H., Simple 3D printed scaffold-removal method for the fabrication of intricate microfluidic devices. *Materials Views, Advanced Science*, **2**, pp. 1–5, 2015.